

# ReWaRD

Version 2.5

## Reference Manual

RETAINING WALL DESIGN

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Set in Optimum using Corel WordPerfect 8.0.

Service Release 2.53 (9/00).

Printed in the UK.

# Acknowledgments

ReWaRD 2.5 was designed and written by Dr Andrew Bond and Ian Spencer of Geocentrix Ltd. The program was originally commissioned by British Steel Ltd.

The *ReWaRD Reference Manual* was written by Dr Andrew Bond.

Parts of ReWaRD were developed with the assistance of Professor David Potts of Imperial College of Science, Technology, and Medicine and Dr Hugh St John of the Geotechnical Consulting Group.

The following people assisted with the testing of this and previous versions of the program: Vassilis Pouloupoulos (Geocentrix); Romain Arnould (Geotechnical Consulting Group); Andy Fenlon (Nonsuch Videographics); Joe Emmerson (British Steel); and Kieran Dineen (Imperial College).



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# Chapter 1

## Introduction

ReWaRD is an advanced program for designing embedded retaining walls under a variety of ground and loading conditions. The program implements a number of techniques for designing retaining walls, including those given in the latest UK and international standards, such as BS 8002 and Eurocode 7.

This chapter of the *ReWaRD Reference Manual* outlines the contents of this book, explains the conventions that are used herein, and tells you what to do if you need help using the program.

### About this book

This *Reference Manual* is divided into the following chapters:

- Chapter 1     *Introduction*
- Chapter 2     *Earth pressures*
- Chapter 3     *Required embedment*
- Chapter 4     *Structural forces*
- Chapter 5     *Peck's envelopes*
- Chapter 6     *Base stability*
- Chapter 7     *Displacements*
- Chapter 8     *Durability*
- Chapter 9     *Safety factors*
- Chapter 10    *Engineering objects*
- Chapter 11    *References*

## Conventions

To help you locate and interpret information easily, the *ReWaRD User Manual* uses the following typographical conventions.

This	Represents
<b>Bold</b>	Items on a menu or in a list-box; the text on a button or next to an edit control; or the label of a group box
<b>Item1 ▶ Item2</b>	An item on a cascading menu. Item1 is the name of an option on the main menu bar (such as <b>File</b> or <b>Window</b> ); and Item2 is the name of an option on the cascading menu that appears when you select Item1 (such as <b>New</b> or <b>Open</b> ). Thus, <b>File ▶ New</b> represents the New command from the File menu.
<i>italic</i>	Place holders for information you must provide. For example, if you are asked to type <i>filename</i> , you should type the actual name for a file instead of the word shown in italics  Italic type also signals a new term. An explanation immediately follows the italicized term
monospaced	Anything you must type on the keyboard
CAPITALS	Directory names, filenames, and acronyms
KEY1+KEY2	An instruction to press and hold down key 1 before pressing key 2. For example, "ALT+ESC" means press and hold down the ALT key before pressing the ESC key. Then release both keys
KEY1, KEY2	An instruction to press and release key 1 before pressing key 2. For example, "ALT, F" means press and release the ALT key before pressing and releasing the F key

## Where to go for help

Your first source of help and information should be the ReWaRD manuals and the on-line help system.

### User manual

The *ReWaRD User Manual* explains how to install and use ReWaRD. It includes a n overview of the program, a tutorial, and separate chapters giving detailed information about ReWaRD's Stockyard and Workbooks.

### Reference manual

The *ReWaRD Reference Manual* (this book) gives detailed information about the calculations ReWaRD performs. The manual assumes you have a working knowledge of the geotechnical design of embedded retaining walls.

### On-line help

The on-line help system contains detailed information about ReWaRD. Help appears in a separate window with its own controls. Help topics that explain how to accomplish a task appear in windows that you can leave displayed while you follow the procedure.

To open the on-line help system:

- Press F1
- Click the Help button in a dialogue box
- Choose a command from the **Help** menu

If you need assistance with using on-line help, choose the **How To Use Help** command from the **Help** menu.

### Tooltips

If you pause while passing the mouse pointer over an object, such as a toolbar button, ReWaRD displays the name of that object. This feature, called Tooltips, makes it easier for you to identify what you see and to find what you need.

## Technical support

Technical support for ReWaRD is available direct from Geocentrix or through your local distributor. If you require technical support, please contact Geocentrix by any of these means:

Voice: +44 (0)1737 373963

Fax: +44 (0)1737 373980

E-mail: [support@geocentrix.co.uk](mailto:support@geocentrix.co.uk)

Web: [www.geocentrix.co.uk](http://www.geocentrix.co.uk)

Please be at your computer and have your licence number ready when you call.

Alternatively, you can write to the following address:

ReWaRD Technical Support  
Geocentrix Ltd  
Scenic House  
54 Wilmot Way  
Banstead  
Surrey  
SM7 2PY  
United Kingdom

Please quote your licence number on all correspondence.

## Sales and marketing information

For sales and marketing information about ReWaRD, please contact ReWaRD Sales on the same numbers as above.

## Chapter 2

# Earth pressures

This chapter gives detailed information about the theory and assumptions behind ReWaRD's earth pressure calculations.

In order to calculate earth pressures, ReWaRD divides the ground into a number of discrete *horizons*. Each horizon contains:

- A soil layer (if below ground level on the retained side of the wall or below formation level on the excavated side)
- A maximum of one water table
- A maximum of one prop or anchor
- An unlimited number of surcharges
- An unlimited number of imposed loads

The results of ReWaRD's earth pressure calculations are available at the top and bottom of each horizon and (when present) at any internal *sub-horizons* within the horizon. ReWaRD inserts sub-horizons into an horizon when:

- Earth pressures increase with depth in a non-linear manner (such as when a non-uniform surcharge is applied to the wall)
- Earth pressures are needed for structural force calculations (to ensure sufficient accuracy in the bending moments)

## Earth pressure conditions

ReWaRD allows you to calculate earth pressures for a number of conditions:

- As built
- At the minimum safe embedment
- With maximum safety factors
- At failure

The following paragraphs explains the assumptions that are made for each of these conditions and the table below summarizes these.

Condition	Wall length*	Safety factors**	In equilibrium?
As built	L	$\gamma$	No***
At minimum safe embedment	< L	$\gamma$	Yes
With maximum safety factors	L	$> \gamma$	Yes
At failure	$\ll L$	1.0	Yes

\*L = specified wall length (as used in the construction stage)

\*\* $\gamma$  = specified safety factor (from the selected design standard)

\*\*\*Unless the wall length is selected accordingly

### Earth pressures as built

ReWaRD calculates as-built earth pressures for the specified wall length and safety factors using limiting earth pressure coefficients. As-built earth pressures are not normally in equilibrium: the wall is either unstable (i.e. has too little embedment) or stable (i.e. has sufficient embedment) at limiting conditions.

### Earth pressures at minimum safe embedment

ReWaRD calculates earth pressures at minimum safe embedment by reducing the wall length until the earth pressures are in equilibrium for the specified safety factors, using limiting earth pressure coefficients.

### Earth pressures with maximum safety factors

ReWaRD calculates earth pressures with maximum safety factors by increasing the safety factors until the earth pressures are in equilibrium for the specified wall length, using limiting earth pressure coefficients.

### Earth pressures at failure

ReWaRD calculates earth pressures at failure by reducing the wall length until the earth pressures are in equilibrium with safety factors set to unity, using limiting earth pressure coefficients.

## Stresses in the ground

This section describes the way ReWaRD calculates the stresses acting in the ground, owing to the weight of soil and water:

- Vertical total stress ( $\sigma_v$ )
- Pore water pressure ( $u$ )
- Vertical effective stress ( $\sigma'_v$ )
- Horizontal effective stress ( $\sigma'_h$ )
- Horizontal total stress ( $\sigma_h$ )

### Total or effective stresses?

The following table indicates when ReWaRD calculates earth pressures using total stress or effective stress theory.

Construction stage designated as...	Type of layer...	
	Drained	Undrained
Short-term	Effective stress	Total stress
Long-term	Effective stress	Effective stress

### Vertical total stress

The vertical total stress in an horizon ( $\sigma_v$ ) is calculated from the unit weight and thickness of any soil layers and standing water above the point being considered:

$$\sigma_v = \int_0^z \gamma \, dz + \gamma_w h_{sw}$$

where  $z$  is the depth below the ground surface;  $\gamma$  is the layer's bulk unit weight;  $\gamma_w$  is the unit weight of water; and  $h_{sw}$  is the height of any standing water.

When there is no water table acting in the horizon or the water table is Dry,  $\gamma$  is equal to the soil's *unsaturated* unit weight; otherwise it is equal to the soil's *saturated* unit weight.

## Pore water pressure

### Drained horizons

The pore water pressure ( $u$ ) at a depth ( $z$ ) in a drained horizon is calculated as follows.

If no water table is present or the water table is dry:

$$u = 0$$

If a water table is present and it is hydraulically connected to the overlying water regime:

$$u = u_T + \left(\frac{\partial u}{\partial z}\right)(z - z_T)$$

where  $u_T$  and  $z_T$  are the pore water pressure and depth (respectively) at the top of the horizon; and  $\partial u/\partial z$  is the pore pressure gradient.

If a water table is present but it is *not* hydraulically connected to the overlying water regime:

$$u = u_A + \left(\frac{\partial u}{\partial z}\right)(z - z_W)$$

where  $u_A$  is the ambient pore water pressure specified by the water table;  $z_W$  is the depth of the water table; and  $\partial u/\partial z$  is the pore pressure gradient.

The value of  $\partial u/\partial z$  is determined by the type of water table present in the horizon (see on-line Help).

### Undrained horizons

The pore water pressure in undrained horizons is calculated as for drained horizons, but it is irrelevant to the calculation of total earth pressures and is therefore not displayed.



## Vertical effective stress

### Drained horizons

The vertical effective stress in the horizon ( $\sigma'_v$ ) is given by Terzaghi's equation:

$$\sigma'_v = \sigma_v - u$$

where  $\sigma_v$  is the vertical total stress and  $u$  the pore water pressure at the corresponding depth.

### Undrained horizons

The vertical effective stress in undrained horizons is irrelevant to the calculation of total earth pressures and is therefore not displayed.

## Horizontal effective stress

### Drained horizons

The horizontal effective stress in a drained horizon ( $\sigma'_h$ ) is obtained from the vertical effective stress ( $\sigma'_v$ ) via the equation:

$$\sigma'_h = K\sigma'_v - K_c c'$$

where  $K$  and  $K_c$  are drained earth pressure coefficients and  $c'$  is the soil's effective cohesion.

The value of  $K$  depends on the soil's angle of friction ( $\phi$ ), the angle of wall friction ( $\delta$ ), the dip of the horizon ( $\beta$ ) and the mode of failure (active or passive):

$$K = f(\phi, \delta, \beta, \text{mode of failure})$$

See the section *Earth pressure coefficients* in this chapter for details on the precise form of the function  $f$ .

$K_c$  depends on the value of  $K$  and also the soil's effective cohesion ( $c'$ ), wall adhesion ( $a$ ), and the mode of failure:

$$K_c = \pm 2 \sqrt{K \left(1 + \frac{a}{c'}\right)}$$

where the + sign is used for active conditions and the – sign for passive (Potts & Burland, 1983).

If the retaining wall is a king-post wall, then the earth pressure coefficients below formation level on the excavated side of the wall are calculated as described in Chapter 10 in the section entitled *Retaining Walls*.

### Undrained horizons

The horizontal effective stress in undrained horizons is irrelevant to the calculation of total earth pressures and is not displayed.

## Horizontal total stress

### Drained horizons

In drained horizons, the horizontal total stress ( $\sigma_h$ ) is given by Terzaghi's equation:

$$\sigma_h = \sigma'_h + u$$

where  $\sigma'_h$  is the horizontal effective stress and  $u$  the pore water pressure at the corresponding depth.

### Undrained horizons

In undrained horizons, the horizontal total stress ( $\sigma_h$ ) is given by:

$$\sigma_h = K_u \sigma_v - K_{uc} C_u$$

where  $K_u$  and  $K_{uc}$  are undrained earth pressure coefficients and  $C_u$  the soil's undrained shear strength.

The value of  $K_u$  is 1 in all cases, whereas the value of  $K_{uc}$  depends on the soil's undrained strength ( $C_u$ ), the undrained wall adhesion

( $a_u$ ), and the mode of failure (active or passive):

$$K_{uc} = \pm 2 \sqrt{1 + \frac{a_u}{C_u}}$$

where the + sign is used for active conditions and the – sign for passive.

If the retaining wall is a king-post wall, then the earth pressure coefficients below formation level on the excavated side of the wall are calculated as described Chapter 10 in the section entitled *Retaining Walls*.

## Pressures from surcharges

This section describes the way ReWaRD calculates earth pressures arising from the presence of surcharges.

## Available calculation methods

ReWaRD supports a number of methods for assessing the effects of surcharges, as listed below:

- Boussinesq's theory (see Clayton & Militiski, 1986) [B]
- Hybrid elastic method (*ibid.*) [HE]
- Wedge analysis (see Pappin *et al.*, 1985) [W]
- Krey's method<sup>1</sup> (British Steel Piling Handbook, 1988) [K]
- Terzaghi's method (see CIRIA 104, 1984) [T]

Not every method can be used with every surcharge, as the following table indicates (in this table, the headings correspond to the letters given above in square brackets).

Surcharge type	B	HE	W	K	T
Uniform	Special method not needed				

<sup>1</sup>Recommended for cohesionless, but not necessarily for cohesive,

Surcharge type	B	HE	W	K	T
Area	✓	✓	✓	✓	
Parallel strip	✓	✓	✓	✓	
Perpendicular strip	✓	✓			
Parallel line	✓	✓	✓	✓	✓
Perpendicular line	✓	✓			
Point	✓	✓			✓

## Uniform surcharges

The vertical stress resulting from a uniform surcharge ( $q$ ) is given by:

$$\sigma_{vq} = q$$

For cantilever and high-propped walls, the corresponding horizontal stress is:

$$\sigma_{hq} = K_a q$$

When the wall is low-propped,  $\sigma_{hq} = K_a q$  for depths *above* the level of the prop (or equivalent single-prop) and:

$$\sigma_{hq} = K_i q$$

for depths *below* the level of the prop.

## Parallel strip surcharges

ReWaRD provides four methods of calculating the effects of parallel strip surcharges.

### Boussinesq's theory

The vertical and horizontal stresses resulting from a parallel strip surcharge of magnitude  $q$  are calculated from the equations:

$$\sigma_{vq} = \frac{q}{\pi} [\alpha + \sin\alpha \cos(\alpha + 2\theta)] e_R$$

$$\sigma_{hq} = \frac{q}{\pi} [\alpha - \sin\alpha \cos(\alpha + 2\theta)] e_R$$

where  $\tan(\alpha + \theta) = (x + y)/z$ ;  $\tan \theta = x/z$ ;  $e_R$  is the elastic reflection parameter (see the section entitled *Surcharges* in Chapter 10);  $z$  is the depth below the surcharge;  $x$  is the perpendicular distance between the wall and the nearest edge of the surcharge; and  $y$  is the width of the surcharge.

### Hybrid elastic method

The vertical stress is calculated from Boussinesq's theory and the horizontal stress is given by:

$$\sigma_{hq} = K_a \sigma_{vq}$$

where  $K_a$  is the active earth pressure coefficient for the horizon.

### Wedge analysis

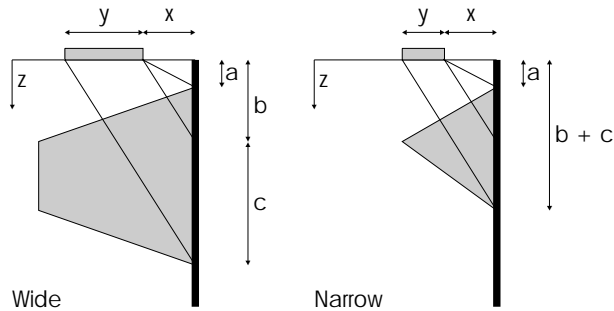
The horizontal stress is calculated from plasticity theory, assuming zero wall friction and adhesion.

The horizontal stress depends on the width of the surcharge. A strip surcharge is considered *wide* if:

$$\frac{2y}{x} \geq 1 + \tan^2 \left( 45^\circ - \frac{\phi}{2} \right)$$

otherwise it is *narrow*. In this equation,  $x$  is the perpendicular distance between the wall and the nearest edge of the surcharge;  $y$  is the width of the surcharge; and  $\phi$  is the soil's angle of friction.

The horizontal stress varies with depth below the surcharge ( $z$ ) as shown below.



For *wide* strip surcharges, the *maximum* horizontal stress is given by:

$$(\sigma_{hq})_{\max} = q \tan^2 \left( 45^\circ - \frac{\phi}{2} \right)$$

and for *narrow* strip surcharges, it is given by:

$$(\sigma_{hq})_{\max} = \frac{4 q \tan^2 \left( 45^\circ - \frac{\phi}{2} \right)}{2 + \frac{x}{y} \left[ 1 + \tan^2 \left( 45^\circ - \frac{\phi}{2} \right) \right]}$$

The vertical stress for both *wide* and *narrow* strip surcharges is assumed to be:

$$\sigma_{vq} = \frac{\sigma_{hq}}{\tan^2(45^\circ - \frac{\phi}{2})}$$

The dimensions  $a$ ,  $b$ , and  $c$  on these diagrams are given by:

$$a = x \tan \phi = \frac{1}{2} b (1 - \tan^2(45^\circ - \frac{\phi}{2}))$$

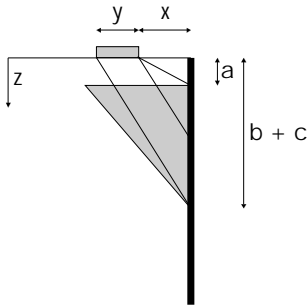
$$b = \frac{x}{\tan(45^\circ - \frac{\phi}{2})}$$

$$c = \frac{y}{\tan(45^\circ - \frac{\phi}{2})}$$

### Krey's method

The horizontal stress is calculated from plasticity theory, assuming zero wall friction and adhesion.

The horizontal stress varies with depth below the surcharge ( $z$ ) as shown below.



The *maximum* horizontal stress is given by:

$$(\sigma_{hq})_{\max} = \frac{4 q \tan^2 \left(45^\circ - \frac{\phi}{2}\right)}{2 + \frac{x}{y} \left[1 + \tan^2 \left(45^\circ - \frac{\phi}{2}\right)\right]}$$

The dimensions  $a$ ,  $b$ , and  $c$  on this diagram are the same as for the Wedge analysis.

The vertical stress is assumed to be:

$$\sigma_{vq} = \frac{\sigma_{hq}}{\tan^2 \left(45^\circ - \frac{\phi}{2}\right)}$$

## Perpendicular strip surcharges

ReWaRD provides two methods of calculating the effects of perpendicular strip surcharges.

### Boussinesq's theory

The vertical and horizontal stresses resulting from a perpendicular strip surcharge of magnitude  $q$  are calculated from the equations:



$$\sigma_{vq} = \frac{q}{\pi} [\alpha + \sin \alpha \cos (\alpha + 2\theta)]$$

$$\sigma_{hq} = 2q\nu \frac{\alpha}{\pi}$$

where  $\tan (\alpha + \theta) = (x + y)/z$ ;  $\tan \theta = x/z$ ;  $z$  is the depth below the surcharge;  $x$  is the distance along the wall to the nearest edge of the surcharge;  $y$  is the width of the surcharge; and  $\nu$  is Poisson's ratio.

### Hybrid elastic method

The vertical stress is calculated from Boussinesq's theory, and the horizontal stress is given by:

$$\sigma_{hq} = K_a \sigma_{vq}$$

where  $K_a$  is the active earth pressure coefficient for the horizon.

## Parallel line surcharges

ReWaRD provides five methods of calculating the effects of parallel line surcharges.

### Boussinesq's theory

The vertical and horizontal stresses resulting from a perpendicular line surcharge of magnitude  $Q$  are calculated from the equations:

$$\sigma_{vq} = 2Q \frac{z^3}{\pi R^4} e_R$$

$$\sigma_{hq} = 2Q \frac{x^2 z}{\pi R^4} e_R$$

where  $R^2 = x^2 + z^2$ ;  $e_R$  is the elastic reflection parameter (see the section entitled *Surcharges* in Chapter 10);  $z$  is the depth below the surcharge; and  $x$  is the perpendicular distance between the wall and the surcharge.

### Hybrid elastic method

The vertical stress is calculated from Boussinesq's theory, and the horizontal stress is given by:

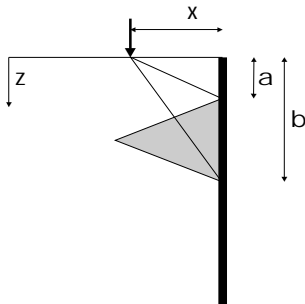
$$\sigma_{hq} = K_a \sigma_{vq}$$

where  $K_a$  is the active earth pressure coefficient for the horizon.

### Wedge analysis

The horizontal stress is calculated from plasticity theory, assuming zero wall friction and adhesion.

The horizontal stress varies with depth below the surcharge ( $z$ ) as shown below.



The *maximum* horizontal stress is given by:

$$(\sigma_{hq})_{\max} = \frac{4 Q \tan^2 (45^\circ - \frac{\phi}{2})}{x [1 + \tan^2 (45^\circ - \frac{\phi}{2})]}$$

The dimensions  $a$  and  $b$  are as defined for parallel strip surcharges.

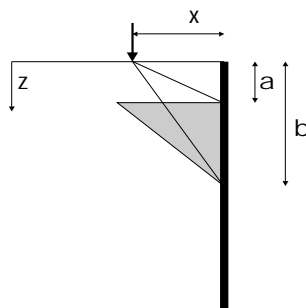
The vertical stress is assumed to be:

$$\sigma_{vq} = \frac{\sigma_{hq}}{\tan^2(45^\circ - \frac{\phi}{2})}$$

### Krey's method

In this method, the horizontal total stress increase is calculated from plasticity theory, assuming zero wall friction and adhesion.

The horizontal stress varies with depth below the surcharge ( $z$ ) as shown below.



The *maximum* horizontal stress is given by:

$$(\sigma_{hq})_{\max} = \frac{4 Q \tan^2 (45^\circ - \frac{\phi}{2})}{x [1 + \tan^2 (45^\circ - \frac{\phi}{2})]}$$

The dimensions  $a$  and  $b$  are the same as for parallel strip surcharges.

The vertical stress is assumed to be:

$$\sigma_{vq} = \frac{\sigma_{hq}}{\tan^2(45^\circ - \frac{\phi}{2})}$$

### Terzaghi's method

Terzaghi's method is based on elasticity theory, modified to match field and model experiments.

The vertical stress is calculated from Boussinesq's theory.

The horizontal stress depends on the proximity of the surcharge to the retaining wall. A line surcharge is considered *near* to the wall if:

$$\frac{x}{H} \leq 0.4$$

otherwise it is *far* from the wall. In this equation,  $x$  is the perpendicular distance between the wall and the surcharge; and  $H$  is the height of excavation below the surcharge.

For *near* line surcharges, the horizontal stress varies with depth below the surcharge ( $z$ ) according to the formula:

$$\sigma_{hq} = 0.20 \frac{Q}{H} \frac{\left(\frac{z}{H}\right)}{\left(0.16 + \left[\frac{z}{H}\right]^2\right)^2}$$

For *far* line surcharges, the horizontal stress varies with depth below the surcharge according to the formula:

$$\sigma_{hq} = 1.28 \frac{Q}{H} \frac{\left(\frac{x}{H}\right)^2 \left(\frac{z}{H}\right)}{\left(\left[\frac{x}{H}\right]^2 + \left[\frac{z}{H}\right]^2\right)^2}$$

## Perpendicular line surcharges

ReWaRD provides two methods of calculating the effects of perpendicular line surcharges.

### Boussinesq's theory

The vertical and horizontal total stresses resulting from a perpendicular line surcharge of magnitude  $Q$  are calculated from the equations:

$$\Delta\sigma_{vq} = 2Q \frac{z^3}{\pi R^4}$$

$$\Delta\sigma_{hq} = 2Q \frac{z}{\pi R^2} \nu$$

where  $R^2 = x^2 + z^2$ ;  $z$  is the depth below the surcharge;  $x$  is the distance along the wall to the surcharge; and  $\nu$  is Poisson's ratio.

### Hybrid elastic method

The vertical stress is calculated from Boussinesq's theory and the horizontal stress is given by:

$$\sigma_{hq} = K_a \sigma_{vq}$$

where  $K_a$  is the active earth pressure coefficient for the horizon.

### Area surcharges

ReWaRD provides four methods of calculating the effects of area surcharges.

#### Boussinesq's theory

The vertical and horizontal stresses resulting from an area surcharge of magnitude  $q$  are calculated from the equations:

$$\sigma_{vq} = \frac{q}{2\pi} \left[ \tan^{-1} \left( \frac{LB}{zR} \right) + \frac{zLB}{R} \left( \frac{1}{R_L^2} + \frac{1}{R_B^2} \right) \right] e_R$$

$$\sigma_{hq} = \frac{q}{2\pi} \left[ \tan^{-1} \left( \frac{LB}{zR} \right) - \frac{zLB}{R} \left( \frac{1}{R_L^2} \right) \right] e_R$$

where  $z$  is the depth below the corner of a rectangular loaded area of length  $L$  and breadth  $B$ ;  $R^2 = z^2 + L^2 + B^2$ ;  $R_L^2 = z^2 + L^2$ ;  $R_B^2 = z^2 + B^2$ ; and  $e_R$  is elastic reflection parameter (see the section entitled *Surcharges* in Chapter 10).

The effect of an area surcharge which is offset from the wall is calculated by superimposing the following surcharges:

- Add stress from area surcharge with  $B = x + y$ ,  $L = v + w$
- Deduct stress from area surcharge with  $B = x$ ,  $L = v + w$
- Deduct stress from area surcharge with  $B = x + y$ ,  $L = v$
- Add stress from area surcharge with  $B = x$ ,  $L = v$

where  $x$  is the perpendicular distance between the wall and the nearest edge of the surcharge;  $y$  is the breadth of the surcharge perpendicular to the wall;  $v$  is the distance parallel to the wall between the cross-section being considered and the nearest edge of the surcharge; and  $w$  is the length of the surcharge parallel to the wall.

### Hybrid elastic method

The vertical stress is calculated from Boussinesq's theory and the horizontal stress is given by:

$$\sigma_{hq} = K_a \sigma_{vq}$$

where  $K_a$  is the active earth pressure coefficient.

### Krey's method and Wedge analysis

In both these methods, the horizontal stress is calculated for a strip surcharge running parallel to the wall, and is then reduced to account for the finite length of the surcharge.

For  $v \leq x$ :

$$(\sigma_{hq})_{AREA} = (\sigma_{hq})_{STRIP} \div \left( \frac{2x}{w} + 1 \right)$$

where  $v$ ,  $x$ , and  $w$  are as defined above.

For  $v > x$ :

$$(\sigma_{hq})_{AREA} = 0$$

The vertical stress is assumed to be:

$$\sigma_{vq} = \frac{\sigma_{hq}}{\tan^2(45^\circ - \frac{\phi}{2})}$$

## Point surcharges

ReWaRD provides three methods of calculating the effects of area surcharges.

### Boussinesq's theory

The vertical and horizontal stresses resulting from a point surcharge of magnitude P are calculated from the equations:

$$\sigma_{vq} = \frac{3Pz^3}{2\pi R^5} e_R$$

$$\sigma_{hq} = \frac{P}{2\pi R^2} \left[ \frac{3z(v^2 + x^2)}{R^3} - (1 - 2\nu)\frac{R}{(R + z)} \right] e_R$$

where  $R^2 = v^2 + x^2 + z^2$ ;  $e_R$  is elastic reflection parameter (see the section entitled *Surcharges* in Chapter 10);  $z$  is the depth below the surcharge;  $v$  is the distance along the wall to the surcharge;  $x$  is the perpendicular distance between the wall and the surcharge; and  $\nu$  is Poisson's ratio.

### Hybrid elastic method

The vertical stress is calculated from Boussinesq's theory, and the horizontal stress is given by:

$$\sigma_{hq} = K_a \sigma_{vq}$$

where  $K_a$  is the active earth pressure coefficient.



### Terzaghi's method

Terzaghi's method is based on elasticity theory, modified to match field and model experiments.

The vertical stress is calculated from Boussinesq's theory.

The horizontal stress depends on the proximity of the surcharge to the retaining wall. A point surcharge is considered *near* to the wall if:

$$\frac{x}{H} \leq 0.4$$

otherwise it is *far* from the wall. In this equation,  $x$  is the perpendicular distance between the wall and the surcharge; and  $H$  is the height of the excavation below the surcharge.

For *near* point surcharges, the horizontal stress varies with depth below the surcharge ( $z$ ) according to the formula:

$$\sigma_{hq} = 0.28 \frac{P}{H^2} \frac{\left(\frac{z}{H}\right)^2}{\left(0.16 + \left[\frac{z}{H}\right]^2\right)^3} \cos^2(1.1\Theta)$$

For *far* point surcharges, the horizontal stress varies with depth according to the formula:

$$\sigma_{hq} = 1.77 \frac{P}{H^2} \frac{\left(\frac{x}{H}\right)^2 \left(\frac{z}{H}\right)^2}{\left(\left[\frac{x}{H}\right]^2 + \left[\frac{z}{H}\right]^2\right)^3} \cos^2(1.1\Theta)$$

In these equations,  $\Theta = \tan^{-1}(v/x)$ , where  $v$  is the distance along the

wall to the surcharge.

## Design pressures

Design pressures acting on the wall are obtained from the series of calculations described below. Appropriate safety factors (see Chapter 9) are included in these calculations depending on which design standard is selected.

## Soil pressures

Earth pressures resulting from the weight of soil alone are termed *soil pressures* in ReWaRD and given the symbol  $E_s$ .

### Drained horizons

Unfactored soil pressures in drained horizons are given by:

$$E_s = \sigma'_h$$

where  $\sigma'_h$  is the horizontal effective stress in the soil.

Design soil pressures are given by:

$$E_{sd} = \frac{E_s}{f_{Es}}$$

where  $f_{Es}$  is the appropriate safety factor for the selected design standard (see Chapter 9).

### Undrained horizons

Unfactored soil pressures in undrained horizons are given by:

$$E_s = \sigma_h$$

where  $\sigma_h$  is the horizontal total stress in the soil.

Design soil pressures are obtained in the same way as for drained

horizons.

## Surcharge pressures

Earth pressures resulting from the presence of surcharges alone are termed *surcharge pressures* in ReWaRD and given the symbol  $E_q$ .

Unfactored surcharge pressures are given by:

$$E_q = \sigma_{hq}$$

where  $\sigma_{hq}$  is the horizontal pressure resulting from any surcharges.

Design surcharge pressures are given by:

$$E_{qd} = \frac{E_q}{f_{Eq}}$$

where  $f_{Eq}$  is the appropriate safety factor for the selected design standard (see Chapter 9).

## Combined earth pressures

The combined earth pressures ( $E$ ) from the weight of soil ( $E_s$ ) and the presence of surcharges ( $E_q$ ) are given by:

$$E = E_s + E_q$$

If the combined earth pressures are negative and the horizon cannot sustain tension (see the section on *Layers* in Chapter 10), then:

$$E = 0$$

If the design total pressure acting in the horizon on the retained side of the wall is less than the minimum active pressure ( $P_{\min}^{\text{ret}}$ , see

below), the design earth pressure  $E_d$  is increased so that:

$$E_d = P_{\min} - W_d$$

where  $W_d$  is the design water pressure acting in the horizon on the retained side of the wall (see below).

## Groundwater pressures

Water pressures resulting from pore water pressures in the soil are termed *groundwater pressures* in ReWaRD and given the symbol  $W_s$ .

### Drained horizons

Groundwater pressures in drained horizons are given by:

$$W_{sd} = W_s = u$$

where  $u$  is the pore pressure in the soil.

### Undrained horizons

Groundwater pressures in undrained horizons are given by:

$$W_{sd} = W_s = 0$$

## Tension cracks

Tension cracks may form on the retained side of the wall when the combined earth pressure  $E$  is negative and the horizon cannot sustain tension. Whether an horizon can sustain tension or not depends on the properties of the layer contained in that horizon (see the section on *Layers* in Chapter 10).

Tension cracks may be dry, wet, or flooded (see the section on *Layers* in Chapter 9) and are limited in extent to whatever depth is specified in the selected design standard (see Chapter 9).

Water pressures resulting from tension cracks are termed *tension*

*crack pressures* in ReWaRD and given the symbol  $W_{tc}$ .

### Dry tension cracks

In dry tension cracks:

$$W_{tc} = 0$$

Dry tension cracks should only be specified if there is no opportunity for water to collect in any tension crack that forms between the wall and the ground.

### Wet tension cracks

In wet tension cracks:

$$W_{tc} = \gamma_w(z - z_{wps})$$

where  $\gamma_w$  is the unit weight of water,  $z$  is the depth below ground surface, and  $z_{wps}$  is the depth of the phreatic surface (i.e. the depth of the uppermost water table).

### Flooded tension cracks

In flooded tension cracks:

$$W_{tc} = \gamma_w z$$

where  $\gamma_w$  and  $z$  are as given above. If the uppermost water table is above ground level (in the case of standing water), then:

$$W_{tc} = \gamma_w(z - z_{wps})$$

where  $z_{wps}$  is negative in value. Flooded tension cracks give the most pessimistic estimate of tension crack pressures.

## Combined water pressures

The combined water pressures ( $W$ ) from the soil ( $W_s$ ) and any tension crack ( $W_{tc}$ ) are given by:

$$W_d = W = \text{maximum of } W_s \text{ and } W_{tc}$$

## Total pressures

Design total pressures are given by:

$$P_d = E_d + W_d$$

If, at any depth on the retained side of the wall, the design total pressure is less than the minimum active pressure (see below), then the design earth pressure is increased so that  $P_d$  equals  $P_{\min}$ .

## Minimum active pressures

The *minimum active pressure* ( $P_{\min}$ ) sets a lower limit to the design total pressure ( $P_d$ ) acting on the retained side of the wall:

$$P_d \nless P_{\min}$$

(CIRIA Report 104 uses the term *minimum equivalent fluid pressure* – “MEFP” – instead of minimum active pressure.)

The minimum active pressure increases with depth ( $z$ ) according to the formula:

$$P_{\min} = M z$$

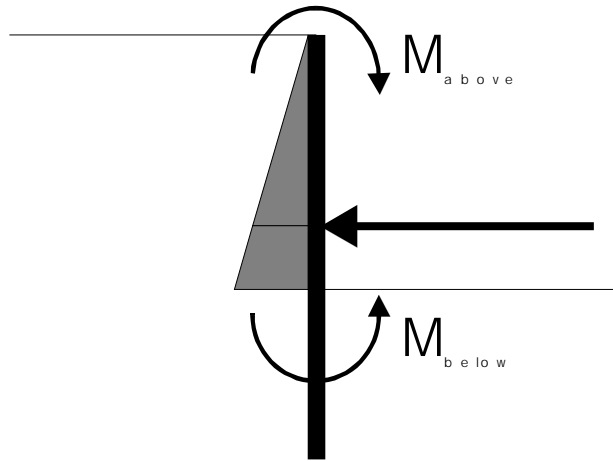
where  $M$  is a constant specified by the selected design standard.

## Low-propped walls

Research at Imperial College (Nyaoro, 1988) has shown that the earth pressures acting on single-propped retaining walls that are

propped at or near excavation level are different to those assumed in conventional limit equilibrium calculations.

A single-propped wall is considered to be *low-propped* if the overturning moment of the total pressures acting on the wall above the prop ( $M_{\text{above}}$ ) exceeds the restoring moment due to the total pressures acting on the wall below the prop *and above excavation level* ( $M_{\text{below}}$ ).



When a wall is low-propped, the wall moves:

- Away from the soil above the prop
- Into the soil below the prop on the retained side of the wall
- Away from the soil below the prop on the excavated side

The corresponding horizontal stresses are calculated using the following earth pressure coefficients:

- Above the prop: active
- Below the prop on the retained side: intermediate between active and passive
- Below the prop on the excavated side: active

### Drained horizons

The earth pressure coefficients in drained horizons are given by:

- $K = K_a$  and  $K_c = K_{ac}$  above the level of the prop

- $K = K_i$  and  $K_c = K_{ic}$  below the level of the prop on the *retained* side
- $K = K_a$  and  $K_c = K_{ac}$  below the level of the prop on the *excavated* side

where the subscripts a and i denote *active* and *intermediate* conditions, respectively.  $K_i$  and  $K_{ic}$  are given by:

$$K_i = K_a + (K_p - K_a) \frac{z_p}{d_p}$$

and

$$K_{ic} = K_{ac} + (-K_{pc} - K_{ac}) \frac{z_p}{d_p}$$

where  $z_p$  is the depth below the level of the prop and  $d_p$  is the depth of the wall toe below the level of the prop.

When  $z_p = 0$ ,  $K_i = K_a$  and  $K_{ic} = K_{ac}$ . When  $z_p = d_p$ ,  $K_i = K_p$  and  $K_{ic} = -K_{pc}$ . The negative sign in front of  $K_{pc}$  ensures that the horizontal effective stress at the toe of the wall equals the full passive pressure, i.e.  $\sigma'_{hi} = K_p \sigma'_v - (-K_{pc})c'$ .

Values of  $K_a$  and  $K_p$  are given in the section in this chapter entitled *Earth pressure coefficients*. Formulae for  $K_{ac}$  and  $K_{pc}$  are given in the section entitled *Stresses in the ground*, under the heading *Horizontal effective stress*.

### Undrained horizons

The earth pressure coefficients in undrained horizons are given by:

- $K_u = 1$  and  $K_{uc} = K_{auc}$  above the level of the prop
- $K_u = 1$  and  $K_{uc} = 1$  and  $K_{uc} = K_{iuc}$  below the level of the prop on the *retained* side
- $K_u = 1$  and  $K_{uc} = K_{auc}$  below the level of the prop on the *excavated* side



where the subscripts a and i denote *active* and *intermediate* conditions, respectively.  $K_{iuc}$  is given by:

$$K_{iuc} = -2 \left(1 - 2 \frac{z_p}{d_p}\right) \sqrt{\left(1 + \frac{a_u}{C_u}\right)}$$

where  $z_p$  is the depth below the level of the prop,  $d_p$  is the depth of the wall toe below the level of the prop,  $C_u$  is the soil's undrained shear strength, and  $a_u$  the undrained wall adhesion.

The formula for  $K_{auc}$  is given in the section in this chapter entitled *Stresses in the ground*, under the heading *Horizontal total stress*.

## Earth pressure coefficients

ReWaRD calculates earth pressure coefficients according to whichever theory is specified in the selected design standard. The earth pressure theories that have been implemented in ReWaRD are those due to:

- Coulomb
- Rankine
- Packshaw
- Caquot & Kerisel
- Kerisel & Absi

## Coulomb

Coulomb (1776) developed an earth pressure theory for rigid (i.e. incompressible) soil which fails on a critical, discrete, planar shear surface. Coulomb's work was later extended by Mayniel (1808) and Müller-Breslau (1906).

ReWaRD calculates Coulomb's earth pressure coefficients using the formulae given by Müller-Breslau (1906) for a frictional cohesionless soil with sloping surface and a frictional wall:

$$K_a = \frac{\sin^2 (90^\circ + \phi) \cos \delta}{\sin (90^\circ - \delta) \left[ 1 + \sqrt{\frac{\sin (\phi + \delta) \sin (\phi - \beta)}{\sin (90^\circ - \delta) \sin (90^\circ + \beta)}} \right]^2}$$

$$K_p = \frac{\sin^2 (90^\circ - \phi) \cos \delta}{\sin (90^\circ + \delta) \left[ 1 - \sqrt{\frac{\sin (\phi + \delta) \sin (\phi + \beta)}{\sin (90^\circ + \delta) \sin (90^\circ + \beta)}} \right]^2}$$

where  $\phi$  = the soil's angle of friction;  $\delta$  = the angle of wall friction; and  $\beta$  = the slope of the soil surface (measured positive upwards).

## Rankine

Rankine (1857) extended earth pressure theory by deriving a solution for a complete soil mass in a state of failure.

ReWaRD calculates Rankine's earth pressure coefficients using the following formulae:

$$K_a = \cos^2 \beta \frac{\cos \beta - \sqrt{(\cos^2 \beta - \cos^2 \phi)}}{\cos \beta + \sqrt{(\cos^2 \beta - \cos^2 \phi)}}$$

$$K_p = \cos^2 \beta \frac{\cos \beta + \sqrt{(\cos^2 \beta - \cos^2 \phi)}}{\cos \beta - \sqrt{(\cos^2 \beta - \cos^2 \phi)}}$$

where the symbols are as given above for Coulomb's theory.

Rankine's theory assumes that the resultant force on a vertical plane acts parallel to the ground surface, and can only be used when the angle of wall friction ( $\delta$ ) equals the ground slope ( $\beta$ ).

The  $\cos \delta$  term in these formulae is replaced by  $\cos \beta$ .

### Packshaw

ReWaRD obtains Packshaw's (1946) earth pressure coefficients from a database of values taken from Code of Practice CP2 (1951).

Account is taken of sloping soil surfaces by increasing the value of  $K_a$  by 1% for every  $1^\circ$  of inclination above the horizontal (as recommended in the British Steel Piling Handbook, 1997). Since  $K_{ac}$  is proportional to the square root of  $K_a$  (see the section entitled *Horizontal effective stress* above), it therefore increases by 0.5% for every  $1^\circ$  of inclination.

### Caquot & Kerisel

Caquot and Kerisel (1948) derived active and passive earth pressure coefficients using log spiral failure surfaces.

ReWaRD calculates Caquot and Kerisel's active earth pressure coefficients from the following formulae:

$$K_a = \rho K_a^{Coulomb}$$

$$\rho = ([1 - 0.9\lambda^2 - 0.1\lambda^4] [1 - 0.3\lambda^3])^{-n}$$

$$n = (2 - \frac{[\tan^2 \beta + \tan^2 \delta]}{2 \tan^2 \phi}) \sqrt{\sin \phi}$$

$$\Delta = 2 \tan^{-1} \left( \frac{|\cotan \delta| - \sqrt{\cotan^2 \delta - \cotan^2 \phi}}{1 + \operatorname{cosec} \phi} \right)$$

$$\lambda = \frac{\Delta + \beta - \Gamma}{4\phi - 2\pi (\Delta + \beta - \Gamma)}$$

$$\Gamma = \sin^{-1} \left( \frac{\sin \beta}{\sin \phi} \right)$$

where  $K_a^{\text{Coulomb}}$  is the value of  $K_a$  from Coulomb's theory.

ReWaRD obtains Caquot and Kerisel's passive earth pressure coefficients from a database of values taken from Clayton & Milititsky (1986).

### Kerisel & Absi

Kerisel and Absi (1990) improved upon the work by Caquot and Kerisel (1948) in deriving active and passive earth pressure coefficients using log spiral failure surfaces.

ReWaRD obtains Kerisel and Absi's passive earth pressure coefficients from a database.

## Chapter 3

# Required embedment

This chapter gives detailed information about how ReWaRD calculates the required embedment of the wall.

### Out-of-balance moment

ReWaRD determines the required embedment of a retaining wall by calculating overturning and restoring moments from the earth pressures acting on it.

The out-of-balance moment ( $\Delta M$ ) is given by:

$$\Delta M = M_R - M_O$$

where  $M_O$  is the overturning moment and  $M_R$  the restoring moment.

The significance of the out-of-balance moment is as follows:

- If  $\Delta M > 0$ , the wall is stable
- If  $\Delta M = 0$ , the wall is in moment equilibrium
- If  $\Delta M < 0$ , the wall is unstable

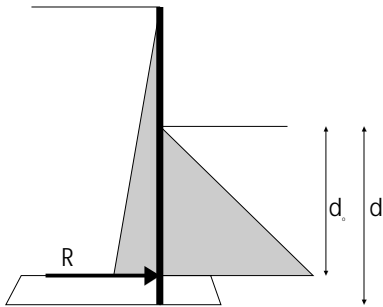
Structural forces cannot be calculated for a wall that is not in moment equilibrium.

### Cantilever walls

ReWaRD determines the required embedment of cantilever walls under fixed-earth conditions.

### Fixed-earth conditions

Under fixed earth conditions, the retaining wall is assumed to rotate about a *pivot* located at some depth ( $d_p$ ) below excavation level. The earth pressures acting on the wall in this situation are as follows.



To simplify the analysis, the earth pressures acting below the pivot are replaced by a single resultant force ( $R$ ). The depth of the pivot below excavation level ( $d_o$ ) is given by:

$$d_o = \frac{d}{1 + C_d}$$

where  $d$  is the total depth of embedment of the wall and  $C_d$  is the *cantilever toe-in*. According to CIRIA Report 104 (1984), a conservative value of  $C_d$  is 20%.

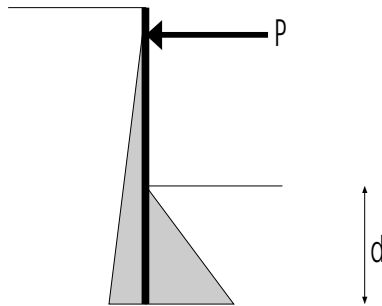
The embedment needed to achieve equilibrium is determined by taking moments about the pivot and occurs when the sum of the (clockwise) overturning moments equals the sum of the (anti-clockwise) restoring moments. The value of  $R$  is found from consideration of horizontal equilibrium.

## Single-propped walls

ReWaRD determines the required embedment of single-propped walls under free-earth conditions.

## Free-earth conditions

Under free-earth conditions, the retaining wall is assumed to rotate about the level of the support. The earth pressures acting on the wall in this situation are as follows:

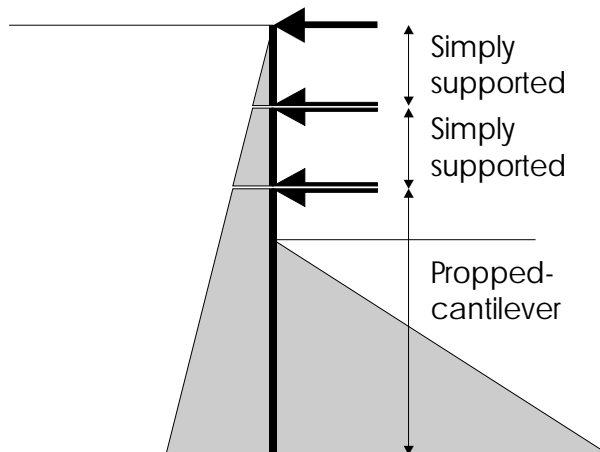


The embedment needed to achieve equilibrium is determined by taking moments about the pivot and occurs when the sum of the (anti-clockwise) overturning moments equals the sum of the (clockwise) restoring moments. The resultant propping force ( $P$ ) is found from consideration of horizontal equilibrium.

## Multi-propped walls

ReWaRD analyses walls with more than one prop using the *hinge method* described in the British Steel Piling Handbook (1997) and BS 8002. In this method, pin joints are introduced at all the support points and the various sections of wall are analysed separately:

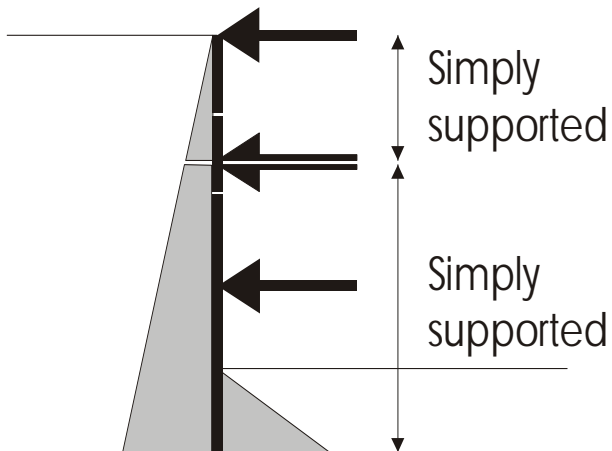
- Sections *between* supports are treated as simply-supported beams
- The lowest section is treated as a single-propped cantilever



The simply-supported sections of the wall are inherently stable, but the propped cantilever section needs sufficient embedment in the ground to prevent the wall toe from kicking into the excavation.

ReWaRD determines the required embedment of a multi-propped wall from the stability of its propped-cantilever section, using the method described above for single-propped walls.

If the propped-cantilever section is unstable, then ReWaRD treats the wall as simply supported (and hence inherently stable) throughout:





## Chapter 4

# Structural forces

This chapter gives detailed information about ReWaRD's structural force calculations.

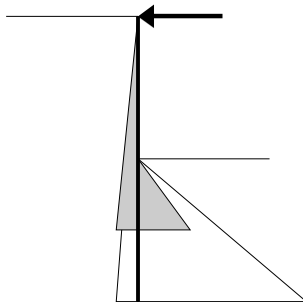
### Cantilever and single-propped walls

Before calculating the structural forces acting in a cantilever or single-propped wall, it is necessary to find a set of earth pressures and applied loads that are in force and moment equilibrium. ReWaRD provides three ways of doing this:

- At minimum safe embedment
- With maximum safety factors
- At failure

#### At minimum safe embedment

In this method, equilibrium is achieved by reducing the depth of embedment of the wall until the earth pressures acting on it are in moment equilibrium. Factors of safety are introduced at appropriate points in the calculations.

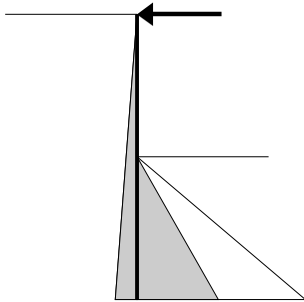


Structural forces calculated by this method are regarded as factored (i.e. design) values (see Chapter 9).

#### With maximum safety factors

In this method, equilibrium is achieved by increasing the factors of safety introduced into the calculations until the earth pressures acting on the wall are in moment equilibrium. The depth of

embedment of the wall is not reduced.



ReWaRD uses the following equation to enhance the safety factors specified in the selected design standard above their normal values:

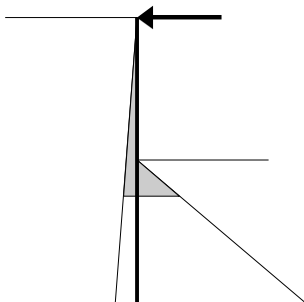
$$f_{\epsilon} = \epsilon(f - 1) + 1$$

where  $f$  is the original safety factor,  $f_{\epsilon}$  the enhanced safety factor, and  $\epsilon$  an enhancement factor. This has been specially formulated to ensure that, when  $f = 1$ ,  $f_{\epsilon} = 1$  and, when  $\epsilon = 1$ ,  $f_{\epsilon} = f$ .

Structural forces calculated by this method are regarded as factored (i.e. design) values (see Chapter 9).

## At failure

In this method, equilibrium is achieved by reducing the depth of embedment of the wall until the earth pressures acting on it are in moment equilibrium. No factors of safety are applied to any part of the calculations.



Structural forces calculated by this method are regarded as

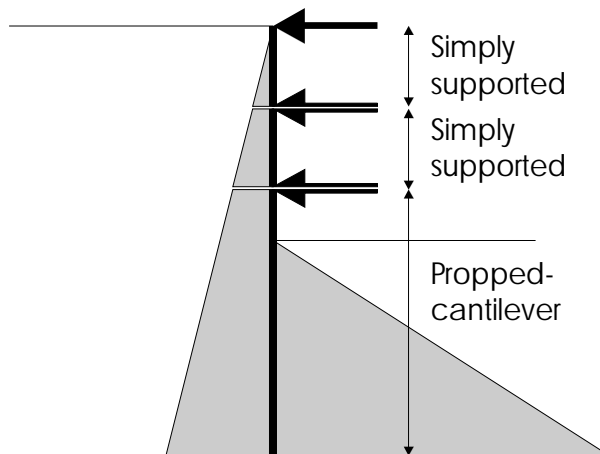
unfactored values and need to be multiplied by an appropriate safety factor to obtain design values (see Chapter 9).

This is the recommended method (Method 1) from CIRIA Report 104 (1984).

## Multi-propped walls

The structural forces acting in a multi-propped wall are calculated by the *hinge method* described in the British Steel Piling Handbook (1997) and BS 8002. In this method, pin joints are introduced at all the support points and the various sections of wall are analysed separately:

- Sections *between* supports are treated as simply-supported beams
- The lowest section is treated as a single-propped cantilever



ReWaRD determines the structural forces in propped-cantilever section using one of the methods described above for cantilever and single-propped walls.

A worked example showing how to use this method is given in CIRIA Special Publication 95 (1993).

## Design structural forces

### Bending moments

Design bending moments ( $M_d$ ) are given by:

$$M_d = f_M M$$

where  $M$  is the unfactored bending moment and  $f_M$  is an appropriate safety factor (see Chapter 9).

### Shear forces

Design shear forces ( $S_d$ ) are given by:

$$S_d = f_S S$$

where  $S$  is the unfactored shear force and  $f_S$  is an appropriate safety factor (see Chapter 9).

### Prop forces

Design prop forces ( $P_d$ ) are given by:

$$P_d = f_p P$$

where  $P$  is the unfactored prop force and  $f_p$  is an appropriate safety factor (see Chapter 9). Different values of  $f_p$  are sometimes used for different props (for double-propped walls, CIRIA 104 recommends a larger  $f_p$  for the upper prop than for the lower prop).

## Chapter 5

# Peck's envelopes

This chapter gives detailed information about ReWaRD's implementation of Peck's envelopes.

### Distributed prop loads

Peck's envelopes provide an empirical way of estimating maximum prop loads for multi-propped walls. The envelopes were derived from measurements of strut loads in real excavations and give the *apparent pressure* acting over the retained height of the wall (Peck, 1968).

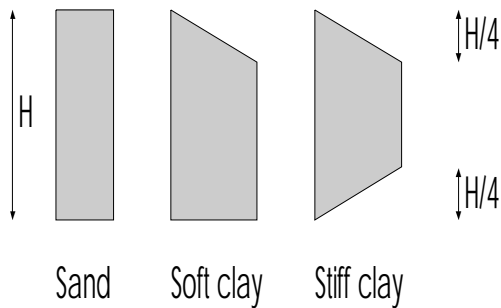
The term *apparent pressure* has misled some people into thinking that Peck's envelopes represent the actual earth pressures acting on the wall. For this reason, and in anticipation of the publication of CIRIA Report RP526, the term *distributed prop load* is used in ReWaRD instead of apparent pressure.

ReWaRD calculates distributed prop loads for multi-propped walls during short-term stages only. At present, only Peck's original envelopes are implemented in the program. When CIRIA Report RP526 is published, support will be added for the envelopes defined in that report. Refer to ReWaRD's release notes and on-line help for further information.

### Peck's envelopes

Peck (1968) introduced envelopes for the following general soil profiles:

- Sand
- Stiff clay
- Soft clay



### Envelope for sand

Peck's envelope for sand is a rectangle (see the diagram above), with the maximum distributed prop load being given by:

$$DPL_{\max} = 0.65 K_a (\sigma'_{vH} + \sigma_{vqH})$$

where  $K_a$  is the average active earth pressure coefficient in any drained horizons existing over the retained height ( $H$ );  $\sigma'_{vH}$  is the vertical effective stress at excavation level on the retained side of the wall; and  $\sigma_{vqH}$  is the vertical surcharge at the same point.

Water pressures in the retained soil (when present) are added to the envelope.

### Envelope for stiff clay

Peck's envelope for stiff clay is a trapezium (see the diagram above), with the maximum distributed prop load being given by:

$$DPL_{\max} = 0.4 (\sigma_{vH} + \sigma_{vqH})$$

where  $\sigma_{vH}$  is the vertical total stress at excavation level on the retained side of the wall and  $\sigma_{vqH}$  is the vertical surcharge at the same point. (Peck's original envelope – which suggested that  $DPL_{\max}$  might be as low as  $0.2[\sigma_{vH} + \sigma_{vqH}]$  – is now considered unconservative.)

Peck's envelope for stiff clay includes the effect of any water

pressures acting on the retained side of the wall and hence water pressures are *not* added to the envelope.

Peck's envelope for stiff clay can only be used when the stability number ( $N$ ) is less than six, as given by:

$$N = \frac{\sigma_{vH} + \sigma_{vqH}}{C_u}$$

where  $C_u$  is the average undrained shear strength in any undrained horizons over the retained height.

### Envelope for soft to medium clays

Peck's envelope for soft to medium clays is a half-trapezium (see the diagram above), with the maximum distributed prop load being given by one of two formulae:

$$DPL_{\max} = \left(1 - \frac{1.6}{N}\right) (\sigma_{vH} + \sigma_{vqH})$$

$$DPL_{\max} = \left(1 - \frac{4}{N}\right) (\sigma_{vH} + \sigma_{vqH})$$

where the symbols are as defined for the stiff clay envelope.

The first formula is used if the cutting is underlain by a deep deposit of soft clay (i.e. when the thickness of soft clay below excavation level exceeds the retained height), otherwise the second equation is used. In this context, clay is considered soft if its undrained strength is less than 40 kPa.

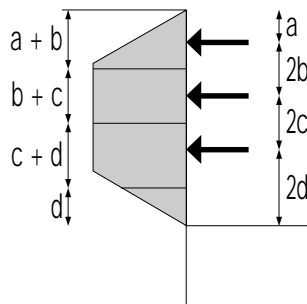
Peck's envelope for soft to medium clays includes the effect of any water pressures acting on the retained side of the wall and hence water pressures are *not* added to the envelope.

Peck's envelope for soft to medium clays can only be used when the stability number  $N$  is greater than four.

## Obtaining prop loads from Peck's envelopes

Prop loads are obtained from Peck's envelopes by dividing the distributed prop load (DPL) diagrams into segments at the midpoints between the props. The load in any one prop is then calculated by integrating the DPL over its associated segment.

The following example illustrates this procedure.



The load carried by the top prop is equal to the area of the first segment, of thickness  $a + b$ .

The load carried by the middle prop is equal to the area of the second segment, of thickness  $b + c$ .

The load carried by the bottom prop is equal to the area of the third segment, of thickness  $c + d$ .

The load represented by the fourth segment is assumed to be carried by the ground below excavation level.



## Chapter 6

# Base stability

This chapter gives detailed information about ReWaRD's base stability calculations.

### Factor-of-safety against basal heave

Bjerrum and Eide (1956) defined the factor-of-safety against basal heave ( $F_{bh}$ ) as follows:

$$F_{bh} = \frac{N_c C_u}{\sigma_{vH} + \sigma_{vqH}^{ret} - \sigma_{vqH}^{exc}}$$

where  $N_c$  is a stability number;  $C_u$  is the average undrained shear strength of any undrained horizons within a depth  $0.7H$  below excavation level;  $H$  is the retained height of the wall;  $\sigma_{vqH}^{ret}$  is the vertical total stress at excavation level on the retained side of the wall;  $\sigma_{vqH}^{exc}$  is the vertical total stress at excavation level on the excavated side of the wall; and  $\sigma_{vH}$  is the vertical surcharge at the same point.

### Stability number

The stability number ( $N_c$ ) is given by:

$$N_c = 9\beta \left| \frac{1 + 0.2B/L}{1.2} \right| \left( \frac{1 + 0.2H/B}{1.5} \right) \text{ for } H/B \leq 2.5$$

$$N_c = 9\beta \left| \frac{1 + 0.2B/L}{1.2} \right| \text{ for } H/B > 2.5$$

where  $H$  is the retained height;  $B$  is the breadth and  $L$  the length of the excavation (see the section on *Excavations* in Chapter 10); and  $\beta$  is the *rigid layer correction* (defined below).

## Rigid layer correction

The rigid layer correction ( $\beta$ ) is derived from the bearing capacity factors given by Button (1953) and is given by:

$$\beta = 1 + 0.008 \left| \frac{d}{B} \right|^{-1.4}$$

where  $d$  is the depth below excavation level to the top of the first rigid layer and  $B$  is the breadth of the excavation.

ReWaRD treats a layer as rigid if it is flagged as such (see the section on *Layers* in Chapter 10).

# Chapter 7

## Displacements

This chapter gives detailed information about ReWaRD's displacement calculations.

ReWaRD estimates the construction-induced (i.e. short-term) movement of the retaining wall – and the settlement of the ground surface behind it – from an extensive database of measured displacements. Long-term movements, which are generally associated with changes in pore water pressure in the soil, are not included in the database but are not usually damaging to the retaining structure. (An exception to this would be in soft clays subject to long-term changes in pore water pressure.)

Displacements depend on a number of factors, of which the most important are the height of the excavation and the prevailing soil type. Dimensionless displacement profiles are used to determine the distribution of movement down and behind the wall.

ReWaRD allows you to view upper bound, average, and lower bound displacements, based on the case histories included in the database.

Displacements are given for sections of wall that deform under plane strain conditions. Sections that are close to the corners of the excavation or close to buttresses, etc., usually displace far less.

### Database of wall movements

ReWaRD's database of measured displacements combines the case histories used by Clough and O'Rourke (1992) and St John *et al.* (1992) to determine construction-induced wall movements.

The database is split into three parts, depending on the prevailing soil conditions:

- Sand
- Stiff clay
- Soft clay

In each case, the measured displacements increase with increasing height of excavation (H), as described below.

## Surcharge loading factor

The *surcharge loading factor* ( $f_q$ ) that appears in many of the equations below takes account of the increase in vertical stress that results from the presence of any surcharges acting on the retained side of the wall.

For sand profiles, the surcharge loading factor is given by:

$$f_q = 1 + \frac{\sigma_{vqH}}{\sigma'_{vH}}$$

where  $\sigma'_{vH}$  is the vertical effective stress at excavation level due to the weight of soil and water and  $\sigma_{vqH}$  is the vertical stress at the same point due to any surcharges.

For soft and stiff clay profiles, the surcharge loading factor is given by:

$$f_q = 1 + \frac{\sigma_{vqH}}{\sigma_{vH}}$$

where  $\sigma_{vH}$  is the vertical total stress at excavation level due to the weight of soil and water and  $\sigma_{vqH}$  is as defined above.

## Database for sands

The database for sands is taken from Clough and O'Rourke (1992) and includes 7 case histories for excavations up to 24m high.

## Cantilever and propped walls

### Maximum displacements

The maximum settlement behind the wall ( $\delta_{vm}$ ) is given by:

$$\frac{\delta_{vm}}{H} = (0.003 \pm 0.001) f_q$$

where  $f_q$  is the surcharge loading factor (see above). The  $\pm$  values represent upper and lower bounds to the data.

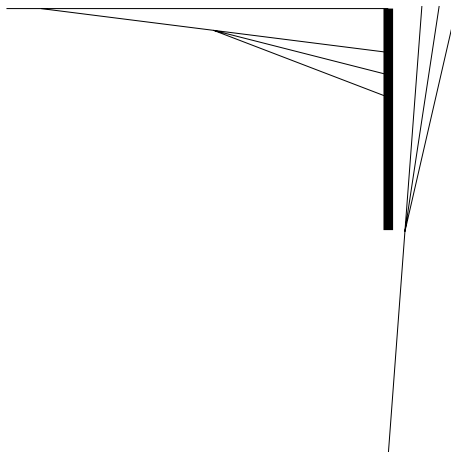
The maximum horizontal movement of the wall ( $\delta_{hm}$ ) is given by:

$$\delta_{hm} = \frac{4}{3} \delta_{vm}$$

### Displacement profiles

Clough and O'Rourke (1992) proposed an envelope of normalized settlement ( $\delta_v/\delta_{vm}$ ) for sands which is triangular and extends for a distance equal to twice the height of the excavation (H).

Closer scrutiny of the data suggests that the bounds to the measured settlements can be defined more closely than Clough and O'Rourke propose. ReWaRD therefore calculates displacements for sands using a modified form of the triangular settlement profile proposed by Clough and O'Rourke, as shown below.



The settlement at  $x = H$  ( $\delta_{vH}$ ) is given by:

$$\frac{\delta_{vH}}{H} = 0.001 f_q$$

and the horizontal displacement at  $z = H$  ( $\delta_{hH}$ ) is given by:

$$\delta_{hH} = \frac{4}{3} \delta_{vH}$$

The same profiles are used for cantilever and propped walls.

## Database for stiff clays

The database for stiff clays is taken from St John *et al.* (1992) and includes 6 case histories involving cantilever excavations up to 8m high and 13 case histories involving propped excavations up to 25m high.

## Cantilever walls

### Maximum displacements

The maximum horizontal movement ( $\delta_{hm}$ ) of a cantilever wall in stiff clay is given by:

$$\frac{\delta_{hm}}{H} = 0.0015 f_q + (0.00035 \pm 0.00025) f_q^2 H$$

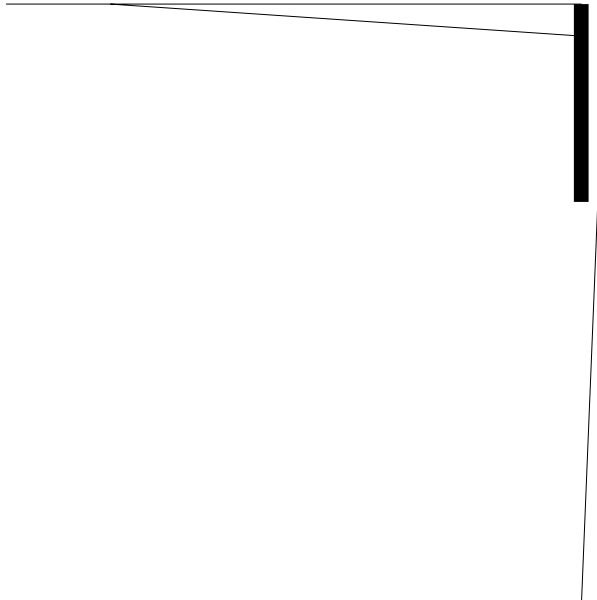
where  $f_q$  is the *surcharge loading factor* (see above). The  $\pm$  values represent upper and lower bounds to the data.

The maximum settlement ( $\delta_{vm}$ ) behind the wall is given by:

$$\delta_{vm} = 0.75 \delta_{hm}$$

### Displacement profiles

Clough and O'Rourke (1992) proposed an envelope of normalized settlement ( $\delta_v/H$ ) for stiff clays which is triangular and extends for a distance equal to three times the height of the excavation ( $H$ ), as shown below.



### Propped walls

#### Maximum displacements

The maximum horizontal movement ( $\delta_{hm}$ ) of a propped wall in stiff clay is given by:

$$\frac{\delta_{hm}}{H} = (0.003 \pm 0.001) f_q$$

where  $f_q$  is the *surcharge loading factor* (see above). The  $\pm$  values represent upper and lower bounds to  $\delta_{hm}$ .

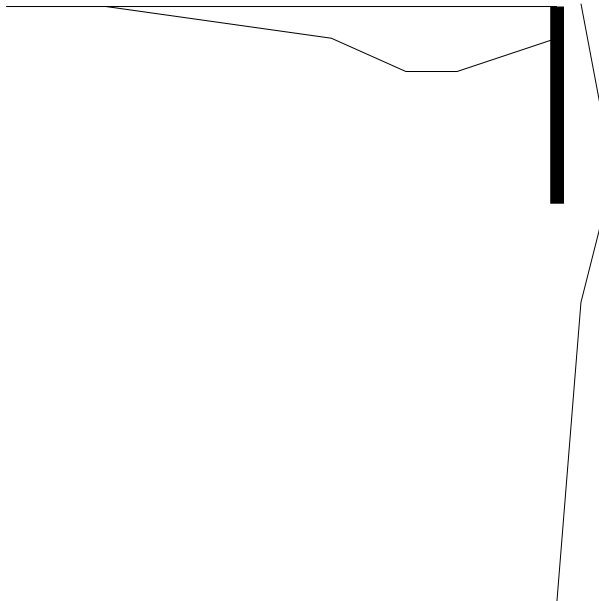
The maximum settlement ( $\delta_{vm}$ ) behind the wall is given by:

$$\delta_{vm} = 0.75 \delta_{hm}$$

### Displacement profiles

As discussed for cantilever walls in stiff clays (above), Clough and O'Rourke (1992) proposed an envelope of normalized settlement ( $\delta_v/H$ ) for stiff clays which is triangular and extends for a distance equal to three times the height of the excavation (H).

St John (1992, personal communication) has found that the maximum settlement behind the wall usually occurs near  $x = H$  and that the settlement close to the wall ( $\delta_{v0}$ ) is approximately 50% of  $\delta_{vm}$ . ReWaRD therefore calculates displacements for propped walls in stiff clays using a modified profile, as shown below.



The table below gives the co-ordinates of the key points along these profiles.



x/H or z/H	0	0.65	1.0	1.5	3.0
$\delta/\delta_m$	0.5	1.0	1.0	0.5	0.0

## Database for soft clays

The database for soft clays is taken from Clough and O'Rourke (1992) and includes 13 case histories for excavations up to 20m high.

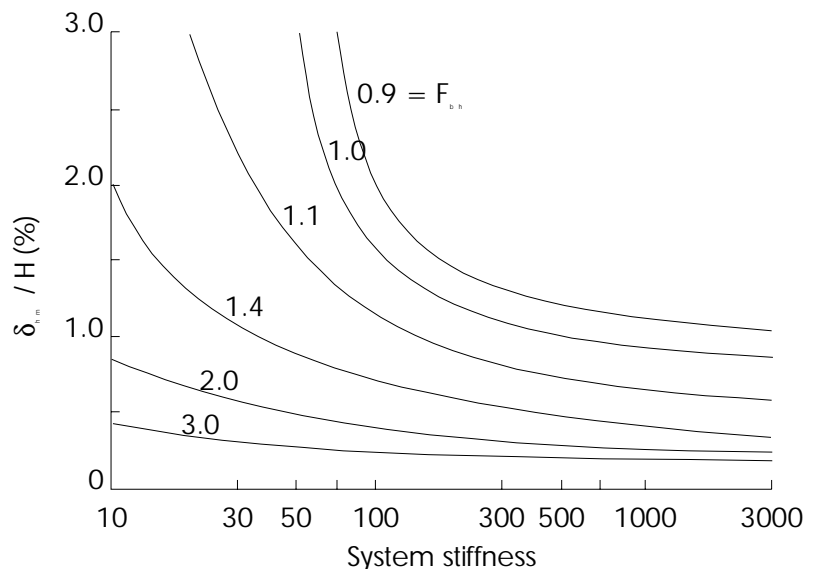
## Cantilever and propped walls

### Maximum displacements

According to Clough *et al.* (1989), the horizontal movements of retaining walls in soft clays is controlled by three main factors:

- The height of the excavation (H)
- The factor-of-safety against basal heave ( $F_{bh}$ , see Chapter 7)
- The system's stiffness ( $EI/\gamma_w S_p^4$ , see below)

Clough *et al.* present design curves that allow the maximum horizontal movement of the wall ( $\delta_{hm}$ ) to be estimated from H,  $F_{bh}$ , and  $EI/\gamma_w S_p^4$  (see below).



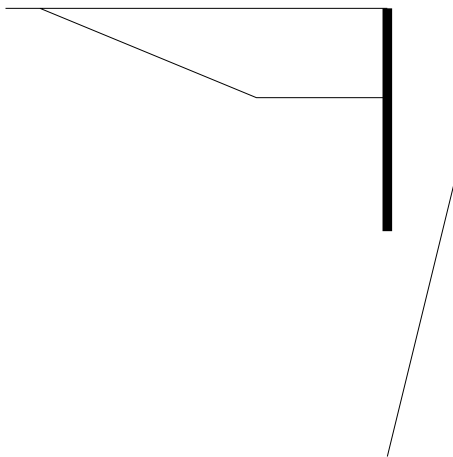
The maximum settlement ( $\delta_{vm}$ ) behind a retaining wall in soft clay is equal in magnitude to its maximum horizontal movement ( $\delta_{hm}$ ) and is given by:

$$\delta_{vm} = \delta_{hm} = f_q \delta_{hm}^{Clough}$$

where  $\delta_{hm}^{Clough}$  is the maximum horizontal movement obtained from Clough *et al.*'s chart.

### Displacement profiles

Clough and O'Rourke propose an envelope of normalized settlement ( $\delta_v/\delta_{vm}$ ) for soft clays which is trapezoidal in shape and extends for a distance equal to twice the height of the excavation (H).



The table below gives the co-ordinates of the key points along these profiles.

x/H or z/H	0	0.75	2.0
$\delta/\delta_m$	1.0	1.0	0.0

The same profiles are used for cantilever and propped walls.

## System stiffness

Clough *et al.* (1989) defined *system stiffness* as follows:

$$\text{System stiffness} = \frac{EI}{\gamma_w s_p^4}$$

where  $E$  is the Young's modulus of the wall and  $I$  its second moment of area;  $\gamma_w$  is the unit weight of water; and  $s_p$  is the *average* spacing between props (a value that can only be calculated for multi-propped walls).

Fernie and Suckling (1996) have suggested a method of defining system stiffness for cantilever and single-propped walls:

- For a cantilever:  $s_p =$  retained height + depth of fixity
- For a single-propped wall:  $s_p =$  (retained height below prop + depth of fixity) *or* retained height above prop (whichever is larger)

Fernie and Suckling further suggest that the depth of fixity ( $d$ ) in soft soils is given by:

- For a cantilever,  $d = 1.4H$
- For a single-propped wall:  $d = 0.6H$

where  $H$  is the retained height.



## Chapter 8

# Durability

This chapter gives information about ReWaRD's durability calculations.

### Corrosion of steel piling in various environments

British Steel's Piling Handbook (1997) gives mean corrosion rates for steel piling in various environments:

Environment	Description	Mean corrosion rate (mm/year)
Atmospheric	Above splash zone	0.035
Splash zone	0 to 1.5 m above tidal zone	0.075
Tidal zone	Between mean high water spring and mean low water neap tides	0.035
Low water zone	Between mean low water neap and lowest astronomical tide levels	0.075
Immersion zone	Between lowest astronomical tide and bed level	0.035
Soil	Below bed level	0.015

ReWaRD calculates the total corrosion rate along a sheet pile wall by summing the mean corrosion rate (taken from the table above) on each side of the wall. For example, a section of wall that is in contact with soil on one side and in the splash zone on the other would have a total corrosion rate of  $0.015 + 0.075 = 0.09$  mm/year.

For further information about durability of sheet pile, refer to Chapter 3 of the Piling Handbook.



## Chapter 9

# Safety factors

This chapter describes the safety factors that ReWaRD uses in its calculation of earth pressures and structural forces.

The following symbols are used throughout this chapter:

$E$  = earth pressure

Subscripts:

$a$  = active mode of failure

$d$  = design (i.e. factored) value

$n$  = nett

$nom$  = nominal value

$p$  = passive mode of failure

$r$  = revised

$u$  = undrained

Superscripts:

$ret$  = retained side of wall

$exc$  = excavated side of wall

## Design approaches

CIRIA Report 104 (1984) discusses two distinct approaches to designing embedded retaining walls, based on:

- A. Moderately conservative soil parameters, loads, and geometry
- B. Worst credible soil parameters, loads, and geometry

Lower factors of safety are appropriate when approach B is adopted.

CIRIA 104 recommends different factors of safety for temporary and permanent works, depending on which design approach is adopted. The following table indicates where factors are quoted in the report.

Design approach	Works	
	Temporary	Permanent
A. Moderately conservative	✓ Effective stress * Total stress	✓ Effective stress ✗ Total stress
B. Worst credible	✓ Effective stress ✗ Total stress	✓ Effective stress ✗ Total stress

✓ = values given; \* = speculative values given; ✗ = values not given

## Safety factors in earth pressure calculations

This section of the *Reference Manual* gives details of the safety factors ReWaRD uses in the earth pressure calculations described in Chapter 2, depending on which design method is adopted:

- Gross pressure method
- Nett pressure method
- Revised (or Burland-Potts) method
- Strength factor method
- Limit state methods

### Gross pressure method

In the *gross pressure method* (described in Civil Engineering Code-of-Practice CP2, 1951), a lumped factor-of-safety ( $F_p$ ) is applied to the gross passive earth pressure:

$$E_{pd} = \frac{E_p}{F_p}$$

Recommended values of  $F_p$  taken from the Literature are given below.



Design standard/approach or reference		Works	
		Temporary	Permanent
CP2		2.0	
Teng (1962)		1.5-2.0	
<i>Canadian Foundation Engineering Manual (1978)</i>		1.5	
CIRIA 104	A. Moderately conservative	$F_p = 1.2-1.5$ for $\phi = 20-30^\circ$ $F_{pu} = 2.0^*$	$F_p = 1.5-2.0$ for $\phi = 20-30^\circ$ $F_{pu} = \mathbf{X}$
	B. Worst credible	$F_p = 1.0$ $F_{pu} = \mathbf{X}$	$F_p = 1.2-1.5$ for $\phi = 20-30^\circ$ $F_{pu} = \mathbf{X}$

\* = speculative;  $\mathbf{X}$  = not given

Burland *et al.* (1981) have criticized the Gross Pressure Method when applied to undrained analysis, because it can lead to two possible required depths of embedment.

## Nett pressure method

In the *nett pressure method* (described in the British Steel Piling Handbook, 1997), a lumped factor-of-safety ( $F_{np}$ ) is applied to the nett passive earth pressure:

$$E_{npd} = \frac{E_{np}}{F_{np}}$$

Recommended values of  $F_{np}$  taken from the Literature are given below.

Design standard	Wall type	
	Cantilever	Propped
British Steel Piling Handbook	1.0*	2.0

\*According to the Piling Handbook, the safety factor is introduced "by the adoption of reasonably conservative soil strength parameters"

Nett earth pressures are given by whichever of the following equations applies:

$$E_n^{ret} = \sigma_h^{ret} - \sigma_h^{exc} \text{ and } E_n^{exc} = 0 \text{ (when } E_n^{ret} \geq 0 \text{)}$$

or:

$$E_n^{ret} = 0 \text{ and } E_n^{exc} = \sigma_h^{exc} - \sigma_h^{ret} \text{ (when } E_n^{exc} > 0 \text{)}$$

Likewise, nett water pressures are given by:

$$W_n^{ret} = u^{ret} - u^{exc} \text{ and } W_n^{exc} = 0 \text{ (when } W_n^{ret} \geq 0 \text{)}$$

or

$$W_n^{ret} = 0 \text{ and } W_n^{exc} = u^{exc} - u^{ret} \text{ (when } W_n^{exc} > 0 \text{)}$$

The nett pressure method has been criticised for giving rapidly increasing factors-of-safety with increasing depth of embedment, and much higher factors-of-safety than other methods (Burland *et al.*, 1981; Potts & Burland, 1983). Results obtained with the nett pressure method should be compared with those from one or more of the other available methods.

## Revised (or Burland-Potts) method

In the *revised (or Burland-Potts) method* (described by Burland *et al.*, 1981), a lumped factor-of-safety ( $F_r$ ) is applied to the revised passive earth pressures below formation level:

$$E_{rpd} = \frac{E_{rp}}{F_r}$$

Recommended values of  $F_r$  taken from the Literature are given below.

Design standard/approach or reference		Works	
		Temporary	Permanent
Burland <i>et al.</i> (1981)		1.5-2.0	
CIRIA 104	A. Moderately conservative	$F_r = 1.3-1.5$ (usually 1.5) $F_{ru} = 2.0$	$F_r = 1.5-2.0$ (usually 2.0) $F_{ru} = \mathbf{X}$
	B. Worst credible	$F_r = 1.0^*$ $F_{ru} = \mathbf{X}$	$F_r = 1.5$ $F_{ru} = \mathbf{X}$

\* = speculative;  $\mathbf{X}$  = not given

## Drained horizons

Revised active earth pressures in drained horizons *below* excavation level are given by:

$$E_{rak} = (K_a \sigma'_{vH})^{ret}$$

where  $K_a$  is the drained active earth pressure coefficient for the horizon on the retained side of the wall and  $\sigma'_{vH}$  is the vertical effective stress on the retained side of the wall at excavation level.

Revised passive earth pressures below excavation level are given by:

$$E_{rpk} = (K_p \sigma'_v + K_{pc} c')^{exc} - (K_a \sigma'_v - K_{ac} c')^{ret} + (K_a \sigma'_{vH})^{ret}$$

where  $K_p$  and  $K_{pc}$  are the drained passive earth pressure coefficients for the horizon on the excavated side of the wall;  $K_a$  and  $K_{ac}$  are the drained active earth pressure coefficients for the horizon on the retained side of the wall; and  $\sigma'_{vH}$  is as defined above.

### Undrained horizons

Revised active earth pressures in undrained horizons *below* excavation level are given by:

$$E_{rak} = (K_{au} \sigma_{vH})^{ret}$$

where  $K_{au}$  is the undrained active earth pressure coefficient for the horizon on the retained side of the wall and  $\sigma_{vH}$  is the vertical total stress on the retained side of the wall at excavation level.

Revised passive earth pressures below excavation level are given by:

$$E_{rpk} = (K_{pu} \sigma_v + K_{puc} C_u)^{exc} - (K_{au} \sigma_v - K_{auc} C_u)^{ret} + (K_{au} \sigma_{vH})^{ret}$$

where  $K_{pu}$  and  $K_{puc}$  are the undrained passive earth pressure coefficients for the horizon on the excavated side of the wall;  $K_{au}$  and  $K_{auc}$  are the undrained active earth pressure coefficients for the horizon on the retained side of the wall; and  $\sigma_{vH}$  is as defined above.

## Strength factor method

In the *strength factor method* (described in CIRIA Report 104, 1984), a factor-of-safety ( $F_s$ ) is applied to the soil's coefficient of friction ( $\tan \phi$ ) and effective cohesion ( $c'$ ) and a different factor-of-safety ( $F_{su}$ ) is applied to its undrained shear strength ( $C_u$ ):

$$\tan \phi_d = \frac{\tan \phi}{F_s}, c'_d = \frac{c'}{F_s}, C_{ud} = \frac{C_u}{F_{su}}$$

The design earth pressures acting in the ground are then calculated from the design soil parameters:

$$E_d = E = f(\phi_d, c'_d, C_{ud}, \dots)$$

Recommended values of  $F_s$  taken from the Literature are given below.

Design standard/approach		Works	
		Temporary	Permanent
CIRIA 104	A. Moderately conservative	$F_s = 1.1$ for $\phi > 30^\circ$ else $F_s = 1.2$ $F_{su} = 1.5^*$	$F_s = 1.2$ for $\phi > 30^\circ$ else $F_s = 1.5$ $F_{su} = \mathbf{X}$
	B. Worst credible	$F_s = 1.0$ $F_{su} = \mathbf{X}$	$F_s = 1.2$ $F_{su} = \mathbf{X}$

\* = speculative;  $\mathbf{X}$  = not given

## Limit state methods

In design standards that employ limit state methods – such as Geoguide 1, BS 8002, and Eurocode 7 – partial factors ( $\gamma$ ) are applied at different stages in the earth pressure calculations.

Partial factors are typically applied to:

- Actions (i.e. direct and indirect loads)
- Material properties
- Geometric properties

### Partial factors on actions

Design actions ( $F_d$ ) are obtained from characteristic actions ( $F_k$ ) by multiplying by the appropriate partial factor ( $\gamma_f$ ):

$$F_d = \gamma_F F_k$$

where the value of  $\gamma_F$  varies from one action to another and depends on the selected design standard.

Recommended values of  $\gamma_F$  taken from the Literature are given below.

Design standard/case		Action			
		Permanent		Variable	Accidental
		Unfav.	Fav.		
Geoguide 1		1.5 on surcharge on retained side of wall, otherwise 1.0			
BS 8002		1.0			
Eurocode 7	A	1.0	0.95	1.5	1.0
	B	1.35	1.0	1.5	1.0
	C	1.0	1.0	1.3	1.0
	Serviceability	1.0	1.0	1.0	1.0

Unfav. = unfavourable; Fav. = favourable

In applying the partial factors from Eurocode 7, pressures arising from the weight of the soil are regarded as unfavourable permanent actions, as are water pressures. Pressures arising from surcharges are regarded as permanent, variable, or accidental and favourable or unfavourable according to which flags are set for each individual surcharge.

### Partial factors on material properties

Design material properties ( $X_d$ ) are obtained from characteristic material properties ( $X_k$ ) by dividing by the appropriate partial factor ( $\gamma_m$ ):

$$X_d = \frac{X_k}{\gamma_m}$$

where different values of  $\gamma_m$  apply to each material property. For soil strength parameters, the specific equations used are:

$$\tan \phi_d = \frac{\tan \phi_k}{\gamma_\phi}, c'_d = \frac{c'_k}{\gamma_c}, c_{ud} = \frac{c_{uk}}{\gamma_{Cu}}$$

where  $\gamma_\phi$ ,  $\gamma_c$ , and  $\gamma_{Cu}$  depend on the selected design standard.

Recommended values of  $\gamma_m$  taken from the Literature are given below.

Design standard/case		Partial factor		
		$\gamma_\phi$	$\gamma_c$	$\gamma_{Cu}$
Geoguide 1		1.2		2.0
BS 8002		1.2		1.5
Eurocode 7	A	1.1	1.3	1.2
	B	1.0		
	C	1.25	1.6	1.4
	Serviceability	1.0		

### Partial factors on geometric properties

The design retained height of the wall ( $H_d$ ) is obtained from the actual retained height ( $H_k$  or  $H_{nom}$ ) by adding an appropriate safety margin ( $\Delta_H$ ):

$$H_d = H_k \pm \Delta_H$$

Recommended values of  $\Delta_H$  taken from the Literature are given below.

Design standard/case		Unplanned excavation ( $\Delta_H$ )
Geoguide 1		None
BS 8002		10% of the clear height*, but a <i>minimum</i> of 0.5m
Eurocode 7	A, B, & C	10% of the clear height*, but a <i>maximum</i> of 0.5m
	Serviceability	None

\*For propped walls, clear height = height below bottom prop  
For cantilever walls, clear height = height of excavation

### Design earth pressures

Design earth pressures acting in the ground are calculated from the design parameters:

$$E_d = E_k = f(F_{d'} \phi_{d'} c_{d'}' C_{ud'} H_{d'} \dots)$$

## Safety factors for structural forces

This section gives details of the safety factors that are applied to the structural force calculations described in Chapter 4.

### At minimum safe embedment

Structural forces calculated at minimum safe embedment (see Chapter 4) are regarded as factored (i.e. design) values.

### Bending moments and shear forces

Design bending moments (M) and shear forces (S) are given by:

$$M_d = M \text{ and } S_d = S$$



**Prop forces**

Design prop forces (P) are given by:

$$P_d = P$$

**With maximum safety factors**

Structural forces calculated with maximum safety factors (see Chapter 4) are regarded as factored (i.e. design) values.

**Bending moments and shear forces**

Design bending moments (M) and shear forces (S) are given by:

$$M_d = M \text{ and } S_d = S$$

**Prop forces**

Design prop forces (P) are given by:

$$P_d = P$$

**At failure**

Structural forces calculated at failure (see Chapter 4) are regarded as unfactored values and need to be multiplied by an appropriate safety factor to obtain design values. (This is equivalent to the “working stress” approach adopted in many of the older codes of practice and is the method recommended in CIRIA Report 104, 1984.)

**Bending moments and shear forces**

Design bending moments (M) and shear forces (S) are given by:

$$M_d = f_M M \text{ and } S_d = f_S S$$

Recommended values of  $f_M$  and  $f_S$  taken from the Literature are given in the table below.

### Prop forces

The design prop force ( $P$ ) for a single-propped wall is given by:

$$P_d = f_p P$$

Recommended values of  $f_p$  taken from the Literature are given in the table below.

Design standard	Safety factor		
	$f_M$	$f_S$	$f_p$
CP2	1.5		$2.0 \times 1.1^* = 2.2$ $2.0 \times 1.15^\dagger = 2.3$
British Steel Piling Handbook	1.5		$2.0 \times 1.15^{*\dagger} = 2.3$
CIRIA 104	1.5		$2.0 \times 1.25^1 = 2.5$ $2.0 \times 1.15^2 = 2.3$

Partial factors to account for arching \*in cohesive soils; †in cohesionless soils; <sup>1</sup>in upper level of props; <sup>2</sup>in second level of props (single- and double-propped walls only)

# Chapter 10

## Engineering objects

This chapter gives detailed information about how the various engineering objects in ReWaRD affect its engineering calculations.

### Construction stages

Construction stages can be designated as short- or long-term. The term helps determine whether ReWaRD calculates earth pressures using total or effective stress theory (see the section entitled *Total or effective stresses?* in Chapter 2).

### Ground profiles

#### Sloping ground

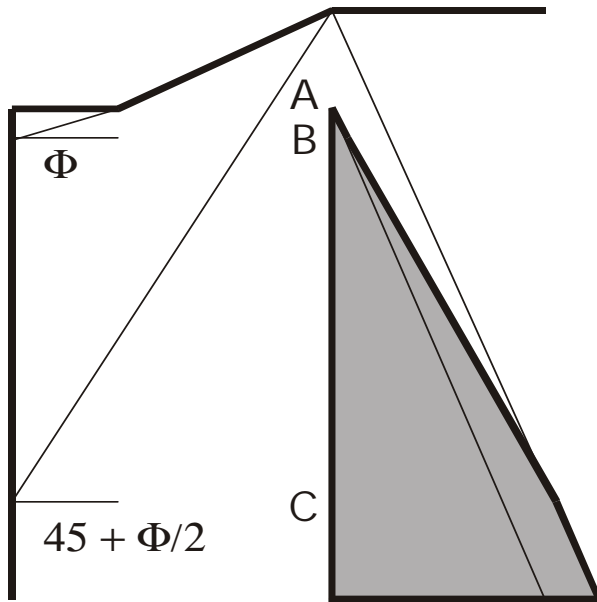
When calculating earth pressure coefficients for horizons on the retained side of the wall, ReWaRD determines the parameter  $\beta$  that appears in the equations for  $K_a$  and  $K_p$  (see Chapter 2) as follows:

$$\beta = \max (\beta_{ground}, i_{layer})$$

where  $\beta_{ground}$  is the slope of the ground profile and  $i_{layer}$  is the dip of the layer for which earth pressure coefficients are being calculated.

#### Stepped ground

The effect of a stepped ground profile is to increase the vertical total stress on the retained side of the wall by an amount that varies with depth as shown below.



The increase in vertical total stress down the wall ( $\Delta\sigma_v$ ) is given by:

$$\Delta\sigma_v = 0 \text{ for } z_a \leq z \leq z_b$$

$$\Delta\sigma_v = \gamma h \frac{z - z_b}{z_c - z_b} \text{ for } z_b < z < z_c$$

$$\Delta\sigma_v = \gamma h \text{ for } z \geq z_c$$

where  $\gamma$  is the unit weight of soil at the ground surface and the depths  $z_b$  and  $z_c$  are given by:

$$z_b = f \tan \phi$$

$$z_c = (w + f) \tan \left( 45^\circ + \frac{\phi}{2} \right) - h$$

where  $\phi$  is the angle of friction of the soil. In these equations,  $h$  is the height,  $w$  the width, and  $f$  the flat of the stepped ground surface.

This approach is identical to the method (C) recommended in CIRIA Special Publication 95 (1993).

## Excavations

### Sloping excavations

When calculating earth pressure coefficients for horizons on the excavated side of the wall, ReWaRD determines the parameter  $\beta$  that appears in the equations for  $K_a$  and  $K_p$  (see Chapter 2) as follows:

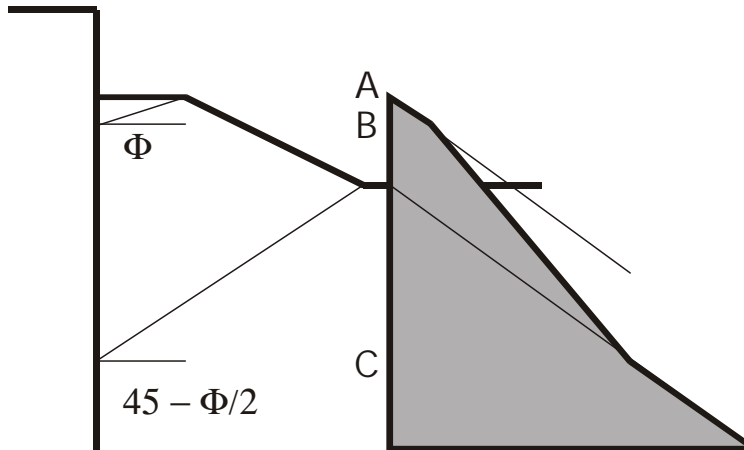
$$\beta = \min (\beta_{excavation}, -i_{layer})$$

where  $\beta_{excavation}$  is the slope of the excavation and  $i_{layer}$  is the dip of the layer for which earth pressure coefficients are being calculated.

### Berms

ReWaRD calculates the effects of a berm on the earth pressures acting on the excavated side of the wall using the method recommended in CIRIA Special Publication 95 (1993).

The effect of the berm is to increase the vertical total stress on the excavated side of the wall by an amount that varies with depth as shown below.



The increase in vertical total stress ( $\Delta\sigma_v$ ) due to the presence of a berm depends on whether it is *wide* or *narrow*.

### Narrow berms

A berm is considered narrow when  $z_b < h$ , in which case  $\Delta\sigma_v$  is given by:

$$\Delta\sigma_v = \gamma z \text{ for } z_a \leq z \leq z_b$$

$$\Delta\sigma_v = \frac{\Delta\sigma_v^{\max}(z - z_b) + \gamma(h - z)z_b}{h - z_b} \text{ for } z_b < z < h$$

$$\Delta\sigma_v = \Delta\sigma_v^{\max} \left[ \frac{z_c - z}{z_c - h} \right] \text{ for } h \leq z < z_c$$

$$\Delta\sigma_v = 0 \text{ for } z \geq z_c$$

where the largest increase in vertical total stress is:

$$\Delta\sigma_v^{\max} = \gamma h \left( \frac{z_c - h}{z_c - z_b} \right)$$

In these equations, all depths are measured from the top of the berm.  $\gamma$  is the unit weight of soil in the berm and the depths  $z_b$  and  $z_c$  are given by:

$$z_b = f \tan \phi$$

$$z_c = (w + f) \tan \left( 45^\circ - \frac{\phi}{2} \right) + h$$

where  $\phi$  is the angle of friction of the soil and  $h$  is the height,  $w$  the width, and  $f$  the flat of the berm.

### Wide berms

A berm is considered narrow when  $z_b \geq h$ , in which case  $\Delta\sigma_v$  is given by:

$$\Delta\sigma_v = \gamma z \text{ for } z_a \leq z \leq h$$

$$\Delta\sigma_v = \gamma h \text{ for } h < z \leq z_b$$

$$\Delta\sigma_v = \gamma h \left[ \frac{z_c - z}{z_c - z_b} \right] \text{ for } z_b \leq z < z_c$$

$$\Delta\sigma_v = 0 \text{ for } z \geq z_c$$

where the symbols are as given for narrow berms.

## Plan dimensions

The plan dimensions of an excavation are used to calculate the factor of safety against basal heave (see Chapter 6).

## Soils

### Soil classification system

ReWaRD's soil classification system is based on a combination of:

- The British Soil Classification System (BSCS), as described in BS 5930:1981
- The Unified Soil Classification System (USCS), as described in ASTM D2487-1069
- The German Soil Classification System (DIN), as described in DIN 18 196

In addition to the basic groupings of Gravel, Sand, Silt, and Clay that are common to all these systems, ReWaRD's Soil Classification system includes commonly-encountered soils under the headings Organic, Fill, Chalk, Rock, River Soil, and Custom.

The following table lists the soils that are included in ReWaRD's soil classification system and give the corresponding group symbols from each of the established systems listed above (where they are available).

	Class	Sym- bol	BSCS	USCS	DIN	States
Gravel	Unclassified*	G	G	G	G	Unspecified (Unsp)
	Well-graded	GW	GW	GW	GW	Very loose (VL)†
	Uniformly-gr'd	GPu	GPu	GP	GE	Loose (L)
	Gap-graded	GPg	GPg	GP	GI	Medium dense (MD)
	Silty	G-M	G-M	G?-GM	GU	Dense (D)
	Clayey*	G-C	G-C	G?-GC	GT	Very dense (VD)
	Very silty*	GM	GM	GM	GU	Poorly comp'd (PC)
	Very clayey*	GC	GC	GC	GT	Well comp'd (WC)



	Class	Sym- bol	BSCS	USCS	DIN	States
Sand	Unclassified*	S	S	S	S	<i>Same as GRAVEL</i>
	Well-graded	SW	SW	SW	SW	
	Uniformly-gr'd	SPu	SPu	SP	SE	
	Gap-graded	SPg	SPg	SP	SI	
	Silty	S-M	S-M	S?-SM	SU	
	Clayey*	S-C	S-C	S?-SC	ST	
	Very silty*	SM	SM	SM	SU	
	Very clayey*	SC	SC	SC	ST	
Granular silt	Unclassified	M	M	M	U	Unpecified (Unsp) Very loose (VL)†¶ Loose (L) Medium dense (MD) Dense (D) Very dense (VD)
	Gravelly	MG	MG	ML/MH	-	
	Sandy	MS	MS	ML/MH	-	
	Low-plasticity	ML	ML	ML	UL	
Cohesive silt	Unclassified*†	M	M	M	U	<i>Same as CLAY</i>
	Int.-plast.*†	MI	MI	ML	UM	
	High-plast.*†	MH	MH-ME	MH	-	
Clay	Unclassified*†\$	C	C	C	T	Unspecified (Unsp)*\$ Very soft (VSo) Soft (So) Firm (F)*\$ Stiff (St)*\$ Very stiff (VSt)*\$ Hard (H)*\$
	Gravelly*†	CG	CG	CL/CH	-	
	Sandy*†	CS	CS	CL/CH	-	
	Low-plast.*†	CL	CL	CL	TL	
	Int.-plast.*†\$	CI	CI	CL	TM	
	High-plast.*†\$	CH	CH-CE	CH	TA	
	Laminated*†	Lam	-	-	-	
Organic	Unclassified†	O	O	O	O	<i>Same as CLAY</i>
	Organic clay†	MO	MLO/ H	OL	(OU)	
	Organic silt†	CO	H	OH	OT	
	Peatt†	Pt	CLO/H	Pt	HN/HZ	
	Loam†	Loam	Pt	-	-	
Granular fill	Unclassified	MdG				Unspecified Poorly-comp'd (PC) Well-compacted (WC)
	Rock fill	RockF				
	Slag fill	Slag				
	Gravel fill	GravF				
	Sand fill	SandF				
	Chalk fill	ChkF				
	Brick hardcore	Brick				
	Ashes	Ash				
	PFA	PFA				
Clay fill†	ClayF				<i>Same as CLAY</i>	

	Class	Sym- bol	BSCS	USCS	DIN	States
Chalk	Unclassified* Grade I* Grade II* Grade III* Grade IV* Grade V Grade VI	Chk Chk1 Chk2 Chk3 Chk4 Chk5 Chk6				Unspecified (Unsp)
Rock	Marl* Weathered rock*	Marl Rock				Unspecified (Unsp)
River soil	River mud† Dock silt† Alluvium†	RivM Dock S Alluv				Unspecified (Unsp) Very soft (VSo) Soft (So)
	Custom*†\$	Cust				Unspecified (Unsp)*\$
G? = G, GW, or GP; S? = S, SW, or SP; Int. = intermediate; plast. = plasticity *may have effective cohesion (if symbol appears next to Class & State) †may be undrained \$may be fissured (if symbol appears next to Class & State) ‡potential for liquefaction						

## Database of soil properties

ReWaRD uses a database of soil properties to check that any parameters you enter for a soil are compatible with that soil's engineering description.

ReWaRD's checking system is based on the concept that there are *normal* and *extreme* ranges for each soil parameter.

If you enter a value that is outside the *extreme* range for a particular soil parameter, ReWaRD issues an error message and prevents you from proceeding until you have changed the offending value.

If you enter a value that is outside the *normal* range, ReWaRD issues a warning message and allows you to proceed only if you confirm that the value entered is correct.

The default parameters are provided to assist in initial design studies only, and should not be used as a substitute for measured

parameters. As in all forms of geotechnical design, parameters should be chosen on the basis of adequate site investigation, including suitable laboratory and field measurements.

The publications that have been referred to in compiling the database include:

- Terzaghi & Peck (1967)
- NAVFAC DM-7 (1971)
- Peck, Hanson, & Thornburn (1974)
- Winterkorn & Fang (1975)
- Canadian Foundation Engineering Manual (1978)
- Reynolds & Steedman (1981)
- Bell (1983)
- Mitchell (1983)
- TradeARBED's *Spundwand-Handbuch Teil 1, Grundlagen* (1986)
- Bolton (1986)
- Clayton & Militiski (1986)
- Clayton (1989)
- Tomlinson (1995)
- British Steel's *Piling Handbook* (1997)

Invaluable advice regarding the properties of various soils was provided by Professors JB Burland, PR Vaughan, and DW Hight and by Dr G Sills.

In the following table  $\rho_d$  = dry density;  $\rho_w$  = wet density;  $\phi_{\text{peak}}$  = peak angle of friction;  $\phi_{\text{crit}}$  = critical state angle of friction;  $c'_{\text{peak}}$  = peak effective cohesion;  $c'_{\text{crit}}$  = critical state effective cohesion;  $S_u$  = undrained shear strength;  $\Delta S_u$  = rate of increase in  $S_u$  with depth.

	Parameter	Classification		Minimum		Default	Maximum	
		Class	State	Ext.	Normal		Normal	Ext.
Gravel	$\rho_d$ (kg/m <sup>3</sup> )	All	Unsp	1200	1400	2050	2200	2500
			VL	1200	1300	1500	1600	1800
			L	1300	1400	1650	1800	2000
			MD	1400	1500	1850	2000	2200
			D	1500	1700	2050	2200	2400
			VD	1700	2000	2250	2400	2500
			PC	1200	1400	1650	1800	2200
			WC	1400	1700	2050	2200	2500

	$\rho_s$ (kg/m <sup>3</sup> )	All	Unsp VL L MD D VD PC WC	1500 1500 1700 1800 1900 2000 1500 1800	1800 1700 1800 1900 2000 2200 1800 2000	2200 1850 2000 2100 2200 2250 2000 2200	2300 1900 2100 2200 2300 2400 2100 2300	2500 2100 2200 2300 2400 2500 2300 2500		
	$\phi_{peak}$ (deg)	All	Unsp VL L MD D VD PC WC	28 28 30 35 40 45 28 35	35 32 35 40 45 50 35 45	37 34 37 42 47 52 37 47	50 38 40 45 50 55 40 50	60 40 45 50 55 60 50 60		
	$\phi_{crit}$ (deg)	All	All	28	35	37	40	45		
	$c'_{peak}$ (kPa)	G G_C GM GC	All	0	0	0	0	10		
		Others	All	Not applicable						
	$c'_{crit}$ (kPa)	G G_C GM GC	All	0	0	0	0	5		
		Others	All	Not applicable						
	Sand	$\rho_d$ (kg/m <sup>3</sup> )	All	Unsp VL L MD D VD PC WC	1200 1200 1225 1275 1350 1450 1200 1275	1275 1225 1275 1350 1450 1575 1275 1450	1675 1450 1500 1575 1675 1800 1500 1675	1800 1550 1600 1700 1800 1900 1600 1800	2200 1750 1850 1950 2050 2200 1950 2200	
			$\rho_s$ (kg/m <sup>3</sup> )	All	Unsp VL L MD D VD PC WC	1600 1600 1750 1800 1850 1950 1600 1800	1800 1750 1800 1850 1950 2050 1800 1950	2075 1900 1950 1975 2075 2175 1950 2075	2150 1975 2000 2050 2150 2250 2000 2150	2400 2000 2050 2150 2250 2400 2150 2400

	$\phi_{peak}$ (deg)	All	Unsp VL	20 20†	30 25†	32 26†	40 28†	55 30†
	†Reduced to allow for potential liquefaction		L MD D VD PC WC	26 29 33 37 23 29	30 33 36 40 30 36	32 34 37 42 32 37	35 37 40 45 35 40	40 45 50 55 45 55
	$\phi_{crit}$ (deg)	All	All	23	30	32	35	40
	$c'_{peak}$ (kPa) discounting natural cementation	S S_C SM SC	All	0	0	0	0	10
		Others	All	Not applicable				
	$c'_{crit}$ (kPa)	S S_C SM SC	All	0	0	0	0	5
		Others	All	Not applicable				
Granular silt	$\rho_d$ (kg/m <sup>3</sup> )	All	All	1100	1275	1850	2150	2200
	$\rho_s$ (kg/m <sup>3</sup> )	All	All	1500	1800	2050	2150	2400
	$\phi_{peak}$ (deg)	All	Unsp VL	20 20†	27 25†	28 26†	33 28†	45 30†
	†Reduced to allow for potential liquefaction		L MD D VD	23 25 27 30	27 28 29 32	28 29 30 33	31 32 33 36	35 37 40 45
	$\phi_{crit}$ (deg)	All	All	20	27	28	31	35
	$c'_{peak}$ (kPa)	All	All	0	0	0	5	10
	$c'_{crit}$ (kPa)	All	All	0	0	0	0	5
	Cohesive silt	$\rho_d$ (kg/m <sup>3</sup> )	All	All	1100	1275	1850	2150
$\rho_s$ (kg/m <sup>3</sup> )		All	All	1500	1800	2050	2150	2400
$\phi_{peak}$ (deg)		M MI MH	All	17 17 17	25 25 20	28 28 23	35 35 30	45 40 35

	$\phi_{crit}$ (deg)	M	All	17	22	25	30	32
		MI		20	22	25	30	32
		MH		17	18	19	22	25
	$c'_{peak}$ (kPa)	All	VSo-So	0	0	0	0	0
			Others	0	0	0	5	10
	$c'_{crit}$ (kPa)	All	VSo-So	0	0	0	0	0
			Others	0	0	0	0	5
	$S_u$ (kPa)	All	Unsp	1	20	20	150	1000
			VSo	1	5	10	20	30
			So	10	20	25	40	60
F			30	40	50	75	100	
St			60	75	100	150	200	
VSt			100	150	200	300	400	
H			200	300	375	500	1000	
$\Delta S_u$ (kPa)	All	VSo-So	-100	-10	0	4	100	
		Others	-100	-10	0	8	100	
Clays	$\rho_d$ (kg/m <sup>3</sup> )	All	Unsp	1200	1500	2050	2200	2500
			VSo	1200	1400	1650	1800	2000
			So	1300	1500	1750	1900	2100
			F	1450	1650	1900	2050	2250
			St	1600	1800	2050	2200	2400
			VSt	1750	1950	2200	2350	2450
			H	1900	2100	2300	2400	2500
	$\rho_s$ (kg/m <sup>3</sup> )	All	Unsp	1200	1500	2050	2200	2500
			VSo	1200	1400	1650	1800	2000
			So	1300	1500	1750	1900	2100
F			1450	1650	1900	2050	2250	
$\phi_{peak}$ (deg)	C CG CS CL CI CH Lam	All	15	20	20	33	39	
			18	20	24	33	39	
			18	20	24	33	39	
			20	24	27	33	39	
			18	20	23	30	37	
			15	16	20	27	31	
			15	16	19	25	39	

	$\phi_{crit}$ (deg)	C	All	8	20	23	33	39	
		CG		18	20	24	33	39	
		CS		18	20	24	33	39	
		CL		18	20	23	28	30	
		CI		18	20	23	28	30	
		CH		8	15	18	20	22	
		Lam		8	12	16	20	22	
	$c'_{peak}$ (kPa)	All	Unsp		0	0	0	10	15
			VSo		0	0	0	0	0
	So			0	0	0	0	0	
		Others		0	0	2	10	15	
$c'_{crit}$ (kPa)	All	VSo-So		0	0	0	0	0	
		Others		0	0	0	0	5	
$C_u$ (kPa)	All	Unsp		1	20	20	150	1000	
		VSo		1	5	10	20	30	
		So		10	20	25	40	60	
		F		30	40	50	75	100	
		St		60	75	100	150	200	
		VSt		100	150	200	300	400	
		H		200	300	375	500	1000	
$\Delta C_u$ (kPa)	All	VSo-So		-100	-10	0	8	100	
		Others		-100	-10	0	8	100	
Organic	$\rho_d$ (kg/m <sup>3</sup> )	Uncl	All	800	1000	1500	2050	2250	
		MO		1000	1250	1500	1600	1750	
		CO		1000	1250	1500	1600	1750	
		Pt		800	1000	1200	1300	1400	
		Loam		1450	1650	1900	2050	2250	
	$\rho_s$ (kg/m <sup>3</sup> )	Uncl	All	850	1050	1650	2050	2250	
		MO		1400	1500	1650	1750	1950	
		CO		1400	1500	1650	1750	1950	
		Pt		850	950	1250	1400	1500	
	Loam		1450	1650	1900	2050	2250		
$\phi_{peak}$ (deg)	Uncl	All	18	20	23	30	39		
	MO		18	20	23	30	37		
	CO		18	20	23	30	37		
	Pt		18	20	23	30	37		
	Loam		20	24	27	33	39		

	$\phi_{crit}$ (deg)	Uncl MO CO Pt Loam	All	18 18 18 18 20	20 20 20 20 24	23 23 23 23 27	30 30 30 30 33	39 37 37 37 39
	$c'_{peak}$ (kPa)	All	All	Not applicable				
	$c'_{crit}$ (kPa)	All	All	Not applicable				
	$C_u$ (kPa)	All	Unsp VSo So F St VSt H	1 1 10 30 60 100 200	20 5 20 40 75 150 300	20 10 25 50 100 200 375	150 20 40 75 150 300 500	1000 30 60 100 200 400 1000
	$\Delta C_u$ (kPa)	All	VSo-So	-100	-10	0	8	100
			Others	-100	-10	0	8	100
Granular fill	$\rho_d$ (kg/m <sup>3</sup> )	MdG	All	600	1225	1600	1800	2500
		RockF		1400	1500	1900	2100	2200
		Slag		1000	1200	1450	1600	1800
		GravF		1200	1400	1950	2200	2500
		SandF		1200	1225	1600	1800	2200
		ChkF		1250	1300	1350	1400	1450
		Brick		1100	1300	1600	1750	1900
		Ash		600	650	1000	1000	1200
		PFA		900	1000	1350	1500	1700
		$\rho_s$ (kg/m <sup>3</sup> )	MdG	All	1200	1650	2000	2150
RockF			1750	1900	2100	2200	2300	
Slag			1400	1700	1850	1900	2000	
GravF			1500	1800	2150	2300	2500	
SandF			1600	1800	2050	2150	2400	
ChkF			1700	1750	1825	1850	1900	
Brick			1400	1650	1850	1950	2100	
Ash			1200	1300	1450	1500	1800	
PFA			1350	1500	1750	1800	2000	
$\phi_{peak}$ (deg)	MdG		All	23	30	35	45	60
	RockF		35	40	43	50	60	
	Slag		25	30	33	40	50	
	GravF		28	35	40	50	60	
	SandF		23	30	32	35	40	
	ChkF		25	30	32	37	43	
	Brick		35	40	42	45	50	
	Ash		30	35	37	40	45	
	PFA		27	30	32	37	40	



	$\phi_{crit}$ (deg)	MdG RockF Slag GravF SandF ChkF Brick Ash PFA	All	25 30 25 28 23 25 25 27 27	30 35 30 35 30 30 30 30 30	32 37 32 37 32 32 32 33 32	35 40 35 40 35 35 35 38 35	45 45 45 45 40 40 40 42 40	
Cohesive fill	$\rho_d$ (kg/m <sup>3</sup> )	All	All	950	1100	1550	1750	1900	
	$\rho_s$ (kg/m <sup>3</sup> )	All	All	1300	1500	1850	2050	2250	
	$\phi_{peak}$ (deg)	All	All	15	17	21	30	35	
	$\phi_{crit}$ (deg)	All	All	15	17	21	28	30	
	$c'_{peak}$ (kPa)	All	All	Not applicable					
	$c'_{crit}$ (kPa)	All	All	Not applicable					
	$C_u$ (kPa)	All	Unsp VSo So F St VSt H	1 1 10 30 60 100 200	20 5 20 40 75 150 300	20 10 25 50 100 200 375	150 20 40 75 150 300 500	1000 30 60 100 200 400 1000	
	$\Delta C_u$ (kPa)	All	VSo-So	-100	-10	0	8	100	
			Others	-100	-10	0	8	100	
Chalk	$\rho_d$ (kg/m <sup>3</sup> )	Chk		1255	1275	1450	2250	2500	
		Chk1		1525	1650	2050	2250	2500	
		Chk2		1350	1400	1575	1650	1725	
		Chk3		1275	1325	1450	1500	1550	
		Chk4		1250	1300	1375	1425	1475	
		Chk5		1225	1275	1350	1400	1450	
		Chk6		1225	1275	1350	1400	1450	
	$\rho_s$ (kg/m <sup>3</sup> )	Chk		1725	1750	1900	2450	2600	
		Chk1		1925	2025	2300	2450	2600	
		Chk2		1800	1850	1975	2025	2075	
		Chk3		1750	1800	1900	1925	1950	
		Chk4		1750	1775	1850	1875	1900	
		Chk6		1725	1750	1825	1850	1900	

	$\phi_{\text{peak}}$ (deg)	Chk		25	30	35	45	55
		Chk1		25	30	35	45	55
		Chk2		25	30	34	43	52
		Chk3		25	30	34	41	49
		Chk4		25	30	33	39	46
		Chk5		25	30	32	37	43
		Chk6		25	30	32	35	40
	$\phi_{\text{crit}}$ (deg)	All		25	30	32	35	40
	$c'_{\text{peak}}$ (kPa)	Chk		0	0	0	20	100
		Chk1		0	0	10	20	100
		Chk2		0	0	5	20	50
		Chk3		0	0	5	20	50
		Chk4		0	0	2	10	20
		Chk5		0	0	0	0	0
		Chk6		0	0	0	0	0
	$c'_{\text{crit}}$ (kPa)	All		0	0	0	0	5
Rock	$\rho_d$ (kg/m <sup>3</sup> )	All		2050	2100	2250	2300	2500
	$\rho_s$ (kg/m <sup>3</sup> )	All		2050	2100	2250	2300	2500
	$\phi_{\text{peak}}$ (deg)	All		27	30	33	38	42
	$\phi_{\text{crit}}$ (deg)	All		27	30	33	38	42
	$c'_{\text{peak}}$ (kPa)	All		0	0	5	10	20
	$c'_{\text{crit}}$ (kPa)	All		0	0	0	0	5
River Soil	$\rho_d$ (kg/m <sup>3</sup> )	All	Unsp VSo So	1200 1200 1200	1250 1250 1400	1600 1600 1650	1800 1800 1800	2000 2000 2000
	$\rho_s$ (kg/m <sup>3</sup> )	All	Unsp VSo So	1200 1200 1200	1250 1250 1400	1600 1600 1650	1800 1800 1800	2000 2000 2000
	$\phi_{\text{peak}}$ (deg)	All	All	15	16	22	33	39
	$\phi_{\text{crit}}$ (deg)	All	All	15	16	22	33	39
	$c'_{\text{peak}}$ (kPa)	All	All	Not applicable				
	$c'_{\text{crit}}$ (kPa)	All	All	Not applicable				
	$C_u$ (kPa)	All	Unsp VSo So	1 1 10	20 5 20	20 10 25	40 20 40	60 30 60
	$\Delta C_u$ (kPa)	All	All	-100	-10	0	4	100

Custom	$\rho_d$ (kg/m <sup>3</sup> )	Uncl	Unsp	600	1200	2000	2400	2500
	$\rho_s$ (kg/m <sup>3</sup> )	Uncl	Unsp	850	1200	2000	2400	2600
	$\phi_{peak}$ (deg)	Uncl	Unsp	10	20	30	50	60
	$\phi_{crit}$ (deg)	Uncl	Unsp	8	20	25	35	45
	$c'_{peak}$ (kPa)	Uncl	Unsp	0	0	0	10	100
	$c'_{crit}$ (kPa)	Uncl	Unsp	0	0	0	0	5
	$C_u$ (kPa)	Uncl	Unsp	1	5	20	300	1000
	$\Delta C_u$ (kPa)	Uncl	Unsp	-100	-10	0	10	100

## Critical state parameters

When calculating earth pressures, ReWaRD applies a partial factor of one to the coefficient of friction and to the effective cohesion of any soil that is flagged as having critical state parameters.

## Fissured soils

Soils that are fissured are not allowed any effective cohesion.

## Layers Dip

When calculating earth pressure coefficients, ReWaRD determines the parameter  $\beta$  that appears in the equations for  $K_a$  and  $K_p$  (see Chapter 2) as follows:

$$\beta^{ret} = \max(\beta_{ground}, i_{layer})$$

$$\beta^{exc} = \min(\beta_{excavation}, -i_{layer})$$

where  $\beta^{ret}$  and  $\beta^{exc}$  are the values of  $\beta$  on the retained and excavated sides of the wall, respectively;  $\beta_{ground}$  is the slope of the ground profile,  $\beta_{excavation}$  is the slope of the excavation; and  $i_{layer}$  is the dip of the layer for which earth pressure coefficients are being calculated.

## Rigid layers

Rigid layers below excavation level can help to increase the factor of safety against basal heave (see Chapter 6). A layer can be considered "rigid" if the ratio of its undrained strength ( $C_u$ ) to that of the overlying layer ( $C_u^{over}$ ) is greater than the threshold values given in the following table. In this table,  $d$  is the depth to the top of the rigid layer and  $B$  is the breadth of the excavation.

$d/B$	1	0.75	0.4	0.3	0.2
$C_u/C_u^{over}$	> 1.2	> 1.5	> 2.0	> 2.5	> 3.0

## Water tables

Water tables represent changes in the groundwater regime. Each water table affects the groundwater conditions in its underlying horizons. When there are several water tables on one side of the wall, the groundwater conditions in any particular soil horizon are determined by the water table at the top of the horizon or immediately above it.

The type of water table that is present in an horizon determines the pore pressure gradient in that horizon and whether the soil is treated as dry or wet when calculating vertical total stresses (see Chapter 2).

Water table	Pore pressure gradient (kPa/m)	Soil below is treated as...
Hydrostatic	9.80665	Wet
Constant	0	Wet
Hydrodynamic	User-defined	Wet
Linear seepage	Program calculates	Wet
Inverted	User-defined	Wet
Dry	0	Dry

Water table	Pore pressure gradient (kPa/m)	Soil below is treated as...
Standing	9.80665	Wet

## Retaining walls

### Section properties

The cross-sectional area (A), second moment of area (I), and section modulus (Z) of the various retaining walls ReWaRD supports are determined as follows.

#### Sheet pile walls

Values of A, I, and Z for Larssen and Frodingham sections are obtained from a database of values supplied by Corus plc.

#### Secant bored-pile walls

$$A = \left(\frac{D^2}{4S}\right) (\pi + \sin 2\theta - 2\theta)$$

$$I = \left(\frac{D^4}{384S}\right) (6\pi - \sin 4\theta + 8 \sin 2\theta - 12\theta)$$

$$Z = \left(\frac{D^3}{192S}\right) (6\pi - \sin 4\theta + 8 \sin 2\theta - 12\theta)$$

where D and S are the pile's diameter and spacing respectively and  $\theta = \cos^{-1}(S/D)$ .

### Contiguous bored-pile walls

$$A = \frac{\pi D^2}{4S}, \quad I = \frac{\pi D^4}{64S}, \quad Z = \frac{\pi D^3}{32S}$$

where D and S are the pile's diameter and spacing respectively.

### King-post (soldier pile) walls

$$A = \frac{\pi D^2}{4S}, \quad I = \frac{\pi D^4}{64S}, \quad Z = \frac{\pi D^3}{32S}$$

where D and S are the pile's diameter and spacing respectively.

### Diaphragm walls

$$A = W, \quad I = \frac{W^3}{12}, \quad Z = \frac{W^2}{6}$$

where W is the wall's width.

### Rowe's parameter

Rowe's parameter is used as a measure of wall flexibility, to determine the effects of moment redistribution. Rowe's parameter ( $\rho$ ) is defined as:

$$\rho = \frac{(L - U)^4}{EI}$$

where L is the overall length of the wall; U is the upstand; E is the wall's Young's modulus; and I is its second moment of area (or inertia) *per unit run*.

## King-post (or soldier-pile) walls

King-post (or soldier-pile) walls mobilize less passive resistance than continuous walls, owing to their horizontal spacing ( $S$ ), which in ReWaRD must be greater than or equal to  $4.5D$ , where  $D$  is the diameter of the pile.

Earth pressure coefficients for king-post walls are calculated from Broms' (1965) theory, as follows.

### Drained horizons

The passive earth pressure coefficients ( $K_p$  and  $K_{pc}$ ) are calculated as described in Chapter 2 (see the section entitled *Earth pressure coefficients*), and then multiplied by a factor  $b$  given by:

$$b = \frac{D}{S}, \text{ for } d < D$$

$$b = \frac{3D}{S}, \text{ for } d \geq D$$

where  $d$  is the depth below excavation level,  $D$  is the diameter of the pile, and  $S$  is the horizontal spacing of the piles.

### Undrained horizons

The passive earth pressure coefficients ( $K_{pu}$  and  $K_{puc}$ ) are given by:

$$K_{pu} = K_{puc} = 0, \text{ for } d < 1.5D$$

$$K_{pu} = 1, K_{puc} = \frac{9D}{S}, \text{ for } d \geq 1.5D$$

where  $d$  is the depth below excavation level,  $D$  is the diameter of the pile, and  $S$  is the horizontal spacing of the piles.

## Surcharges

### Elastic reflection parameter

The *elastic reflection parameter* ( $e_R$ ) that appears in several of the formulae for surcharge pressures in Chapter 2 takes account of the degree of yielding of the wall:

- If the wall is flexible,  $e_R \rightarrow 1$
- If the wall is rigid,  $e_R \rightarrow 2$

The doubling of horizontal stress for rigid walls can be explained as follows. In order to obtain zero horizontal displacements along the line of the wall, an imaginary surcharge is needed on the front side of the wall equal in magnitude and position to the real surcharge on the back. The principle of superposition implies that with two surcharges  $\sigma_{hq}$  will be double what it would have been with just one.

The elastic reflection parameter has been found in experiments to vary between 1.0 and 1.5, depending on how rigid the wall is. According to Schmitt & Gilbert (1992), it is common practice in France to use an elastic reflection parameter between 1.5 and 2.0.

The elastic solutions for perpendicular strip and line loads already include an imaginary surcharge on the front of the wall, and hence implicitly assume that  $e_R = 2$ .

### Duration/effect

The duration (Permanent, Variable, or Accidental) and effect (Favourable or Unfavourable) of a surcharge determine the partial factors that are used in the calculation of design pressures for Eurocode 7 (see Chapter 9).

## Imposed loads

### Duration/effect

The duration of an imposed load (Permanent, Variable, or Accidental) and its effect (Favourable or Unfavourable) determine the partial factors that are used in the calculation of design pressures for Eurocode 7 (see Chapter 9).



# Chapter 11

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